

Thermal Impedance Spectroscopy Method as Applied for Road Bearing Layer Structure Thermoelectric Parameters Determination

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Abstract:

In this article, we propose to determine by thermal electric- analogy of the thermoelectric parameters of a road bearing layer structure from the thermal impedance spectroscopy method.

When the road surface is submitted to thermal constraints, a heat exchange phenomenon appears to be characterized by the radiation thermal exchange coefficient and the convection thermal exchange coefficient. The influence of one of these coefficients compared with the other one on the road depends on its environment (shade or illumination).

The determination of the thermal electric parameters allow the valid bearing layer thermal stability. The method used is the thermal impedance spectroscopy method.

Keywords: Road- thermal impedance spectroscopy- convection thermal exchange coefficient- radiation thermal exchange coefficient.

I. INTRODUCTION

The road structure can be considered as a set of multilayer. A road surface get permanently thermal [1-3] and mechanical constraints [4,5]. Many scientific has been done in the aim of studying the impact of heavy weighted (car) on the road surface dimensioning, from the deformation module and the permissible stresses [6-8].

The noted damages on the road [9,10] appears in the form of cracks or of excessive deformations [11,12].

In zones of high temperature, it is primordial to take in account this phenomenon for the road conception, maintenance and rehabilitation. So, other others has lead there studies in the effect of the temperature on the road’s body [13-16]. The amplitude of this phenomenon depends on several parameters, but specially the soil characteristics (granulate, permeability, chemical physical composition, amount of water, density, level of saturation...)[17] and external factors (weather conditions and water supply) [10].

Scientifique research deals with this problem through modeling and analogic studies. However, the thermal impedance spectroscopy [18-20] seemstoo relevant to the thermal stability of systems.

The aim of this paper is to propose the thermal electric parameters such as the break frequency, the resonance frequency, the series and parallel resistance by thermal electric analogy. This study highlights the convection thermal exchange coefficient [21-22] in shadowed zones, and radiation thermal exchange coefficient [23, 24] in zones under illumination.

II. MODEL STUDY

The studied model is a road structure. Its body consists of a multilayer system composed by an asphalt coat [25] on the surface layer, a crushed gravel material as the based layer, and a raw lateritic foundation. These materials are supported by the based soil as indicated in figure 1.

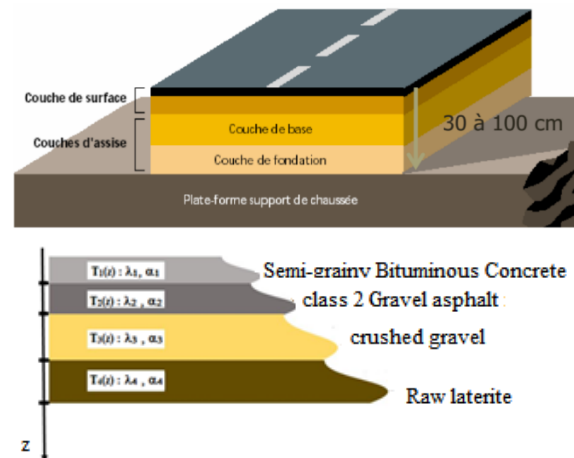


Figure 1: View of the Road Structure

The thickness of the layers is the following:

- Bituminous Semi-Grenu Concrete : 0.05m
- Class 2 Gravel Asphalt: 0.08m
- Crushed Gravel : 0.2m
- Raw Laterite : 0.2m

When the most external layer of the road subjected (submitted) is submitted to thermal constraint (figure 2), we observe then a heat transfer phenomenon from high towards low temperatures.

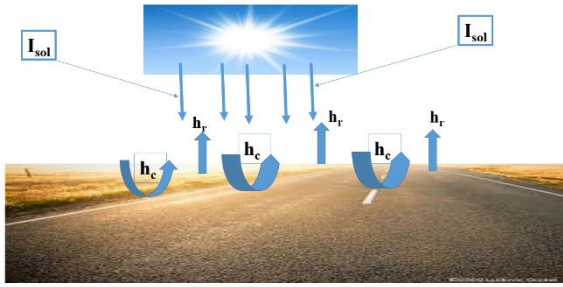


Figure 2: Constraints and Thermal Exchanges on the Asphalt

The indications $i=1,2,3,4$ are respectively attributed from the first to the last layer. To determine the coefficients $A_i(h1, h2, \omega, t, Cn)$ and $B_i(h1, h2, \omega, t, Cn)$, we are going to define the conditions on the borders.

This phenomenon creates thermal exchanges governed by the equation of the heat (1)

$$\frac{\partial^2 T(z, hc, hr, \omega, t, Cn)}{\partial z^2} - \frac{1}{\alpha} \frac{\partial T(z, hc, hr, \omega, t, Cn)}{\partial t} = Pp(1)$$

The heat equations relative to every layer are proposed by considering that there is no internal source of heat:

In the of Semi-grainy Bituminous concrete layer

$$\frac{\partial^2 T_1(z, hc, hr, \omega, t, Cn)}{\partial z^2} - \frac{1}{\alpha_1} \frac{\partial T_1(z, hc, hr, \omega, t, Cn)}{\partial t} = 0(2)$$

In the connection layer of class 2 Gravel Asphalt of

$$\frac{\partial^2 T_2(z, hc, hr, \omega, t, Cn)}{\partial z^2} - \frac{1}{\alpha_2} \frac{\partial T_2(z, hc, hr, \omega, t, Cn)}{\partial t} = 0(3)$$

In the basic layer crushed gravel

$$\frac{\partial^2 T_3(z, h1, h2, \omega, t, Cn)}{\partial z^2} - \frac{1}{\alpha_3} \frac{\partial T_3(z, h1, h2, \omega, t, Cn)}{\partial t} = 0(4)$$

In the layer of foundation in Raw Laterite

$$\frac{\partial^2 T_4(z, h1, h2, \omega, t, Cn)}{\partial z^2} - \frac{1}{\alpha_4} \frac{\partial T_4(z, h1, h2, \omega, t, Cn)}{\partial t} = 0(5)$$

$$\text{With } \alpha_1 = \frac{\lambda_1}{\rho_1 c_1} ; \alpha_2 = \frac{\lambda_2}{\rho_2 c_2} ;$$

$$\alpha_3 = \frac{\lambda_3}{\rho_3 c_3} \text{ and } \alpha_4 = \frac{\lambda_4}{\rho_4 c_4}$$

- ✓ $T_1(z, hc, hr, \omega, t, Cn)$: temperature in a considered point in the Grainy Semi Bituminous Concrete
- ✓ $T_2(z, hc, hr, \omega, t, Cn)$: temperature in a considered point in class 2 Gravel Asphalt
- ✓ $T_3(z, hc, hr, \omega, t, Cn)$: temperature in a considered point in the Crushed Gravel
- ✓ $T_4(z, hc, hr, \omega, t, Cn)$: the temperature in a point considered in the Raw Laterite

However, we meet three types of boundary conditions:

- The boundary conditions told condition imposed flow (problem of Neumann)

- The boundary conditions told condition imposed flow (problem of Neumann)
- The boundary conditions said condition of Fourier or Newton (problem of Fourier)

The heat transfers in this domain are conductive and monodimensional.

In the interface outer environment and the layer of bituminous concrete, a condition of continuity of flows is held:

- ❖ Interface outer environment and the layer of Grainy Semi Bituminous Concrete:

$$-\lambda_1 \frac{\partial T_1(z)}{\partial z} \Big|_{z=0} = hc(Ta1 - T(0)) + hr(T_s - T0 + Isol)(6)$$

- ✓ hc : Coefficient of thermal exchange by convection
- ✓ hr : coefficient of thermal exchange by radiation
- ✓ $Ta1$: ambient temperature of the environment
- ✓ T_s : temperature supplied by the sun in the ambient environment.
- ✓ $Isol$: solar flow arriving on the surface of the first layer

The expression of the solar flow is proposed by the following [11,12] :

$$I_{sol} = (0.828. I + b). (1 - Cn/100)(7)$$

So the cloud layer allows estimate the quantity of light which reaches the surface of the ground.

- ❖ Grave Asphalt of class 2 Interface between the Grainy Semi Bituminous Concrete and crushed gravel:

$$\lambda_1 \frac{\partial T_1(z)}{\partial z} \Big|_{z=L1} = \lambda_2 \frac{\partial T_2(z)}{\partial z} \Big|_{z=L1} (8)$$

$$T_1(L1) = T_2(L1)(9)$$

- ❖ Interface between class 2 Gravel Asphalt and the Crushed Gravel:

$$-\lambda_2 \frac{\partial T_2(z)}{\partial z} \Big|_{z=L2} = -\lambda_3 \frac{\partial T_3(z)}{\partial z} \Big|_{z=L2} (10)$$

$$T_2(L2) = T_3(L2)(11)$$

- ❖ Interface between the Crushed Gravel and the Raw Laterite: :

$$-\lambda_3 \frac{\partial T_3(z)}{\partial z} \Big|_{z=L3} = -\lambda_4 \frac{\partial T_4(z)}{\partial z} \Big|_{z=L3} (12)$$

$$T_3(L3) = T_4(L3) (13)$$

- ❖ Interface between the Raw Laterite and the platform: :

$$-\lambda_4 \frac{\partial T_4(z)}{\partial z} \Big|_{z=L4} = 0(14)$$

$$T_4(L4) = Tp(15)$$

At the initial moment, the temperature in a layer is isothermal. But this initial temperature is not

constant for the set of layers. Indeed we supposed a one degree variation between layers: of the bearing layer to the layer of platform. So, by taking into account this temperature, we proceed to a change of variables

In the layer of Semi-grainy Bituminous concrete rotation

$$\bar{T}_1(z, h1, h2, \omega, t, Cn) = T_1(z, h1, h2, \omega, t, Cn) - T_{i1}$$

In the connection layer of class 2 Gravel Asphalt

$$\bar{T}_2(z, h1, h2, \omega, t, Cn) = T_2(z, h1, h2, \omega, t, Cn) - T_{i2}$$

In the basic layer of crushed gravel

$$\bar{T}_3(z, h1, h2, \omega, t, Cn) = T_3(z, h1, h2, \omega, t, Cn) - T_{i3}$$

In the foundation layer of Raw Laterite

$$\bar{T}_4(z, h1, h2, \omega, t, Cn) = T_4(z, h1, h2, \omega, t, Cn) - T_{i4} \quad (19)$$

The heat equation becomes:

In the layer of Semi-grainy Bituminous concrete

$$\frac{\partial^2 \bar{T}_1(z, h1, h2, \omega, t, Cn)}{\partial z^2} - \frac{1}{\alpha_1} \frac{\partial \bar{T}_1(z, h1, h2, \omega, t, Cn)}{\partial t} = 0 \quad (20)$$

In the class 2 connection layer of Gravel Asphalt

$$\frac{\partial^2 \bar{T}_2(z, h1, h2, \omega, t, Cn)}{\partial z^2} - \frac{1}{\alpha_2} \frac{\partial \bar{T}_2(z, h1, h2, \omega, t, Cn)}{\partial t} = 0 \quad (21)$$

In the basic layer crushed gravel

$$\frac{\partial^2 \bar{T}_3(z, h1, h2, \omega, t, Cn)}{\partial z^2} - \frac{1}{\alpha_3} \frac{\partial \bar{T}_3(z, h1, h2, \omega, t, Cn)}{\partial t} = 0 \quad (22)$$

In the foundation layer in Raw Laterite

$$\frac{\partial^2 \bar{T}_4(z, h1, h2, \omega, t, Cn)}{\partial z^2} - \frac{1}{\alpha_4} \frac{\partial \bar{T}_4(z, h1, h2, \omega, t, Cn)}{\partial t} = 0 \quad (23)$$

The resolution of these equations from the method of separation of variables gives the expression of the additional temperature under the following shape:

$$\bar{T}_i(z, hc, hr, \omega, t, Cn) = (A_i(hc, hr, \omega, t, Cn) \sinh(\beta_1 \cdot z) + B_i(hc, hr, \omega, t, Cn) \cosh(\beta_1 \cdot z)) * e^{j \cdot \omega \cdot t} \quad (24)$$

➤ **Heat density flow and thermal impedance.**

The quantity of per unit square is obtained from the Fourier law by conduction [28-30]:

$$\vec{\phi}_i(z, h1, h2, \omega, t, Cn) = -\lambda_i \cdot \overrightarrow{grad} T_i(z, h1, h2, \omega, t, Cn) \quad (25)$$

In frequency modulation, the dynamic impedance [31] is given in electricity by the following expression:

$$Z_n(\lambda, \omega, S_{f_n}, S_{b_n}) = \frac{V_n(\lambda, \omega, S_{f_n}, S_{b_n})}{J_n(\lambda, \omega, S_{f_n}, S_{b_n})} \quad (26)$$

By analogy, the equivalent [32,33] thermal impedance expression is deduced from two distinct points given by.:

$$Z_{eq}(x, h1, h2, \omega, t) = \frac{\Delta T(x, h1, h2, \omega, t)}{\Phi(x, h1, h2, \omega, t)} \quad (27)$$

We shall note the correspondence existence between thermal electric parameters. The following table illustrates these relations:

Table 1 : Correspondence Between Thermal Electric Parameters

ELECTRIC PARAMETERS	THERMIC PARAMETERS
Potential difference (Volt) : ΔV	Temperature difference (°C) : ΔT
Current density (A.m⁻²) : $J = \frac{dq}{dt}$	Heat flow density (W.m ⁻²) : $\vec{\Phi} = -\lambda grad T$ (18)
Electric impedance (W) : $Z = \frac{\Delta V}{J}$	Thermal impedance (K/W.m ⁻²) : $Z_{eq} = \frac{\Delta T}{\Phi}$
Current intensity (A) : I	Heat flow (W) : ϕ

III. RESULTS AND DISCUSSIONS

A. Bode Diagram of the Thermal Equivalence Impedance

The figures 3 and 4, give the thermal equivalence module under influence the radiation thermal exchange coefficient and the convection thermal exchange. These curves give the break frequency, the resonance frequency, and highlight the frequency band regime.

Indeed, for long solicitation periods (weak pulse values), the equivalence thermal impedance is so low that seems to be constant as a statistic regime. A part from some values called break frequency, it is noticed a rise of the thermal impedance reaching a maximum and decrease. This part in the curve, correspond to dynamic regime.

Tables 2 and 3 give the break frequency values, the resonance, the equivalent thermal impedance module maximum amplitude.

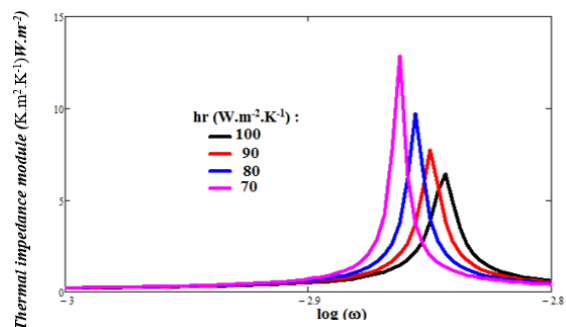


Figure 3: Equivalent Thermal Impedance Module According to the Decimal Logarithm of the Pulse. Hc=0.01W.M⁻².K⁻¹, I=800W.M⁻², Z=0.05m

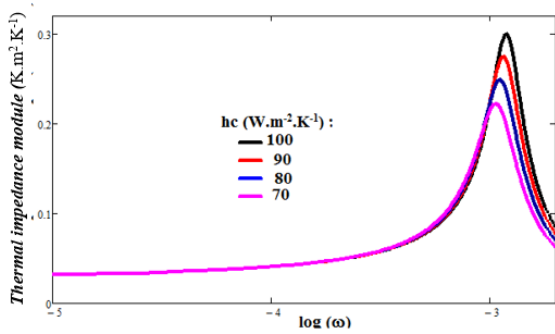


Figure 4:Equivalent Thermal Impedance Module According to the Decimal Logarithm of the Pulse
Hr=0.01W.M⁻².K⁻¹, I=800W.M⁻², Z=0.05m

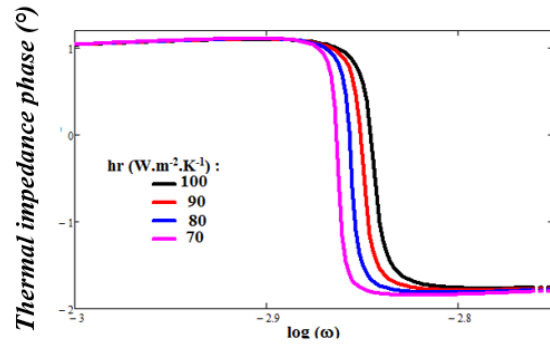


Figure 5: Equivalent Thermal Impedance Phase According to the Decimal Logarithm of the Pulse.
Hc=0.01W.M⁻².K⁻¹, I=800W.M⁻², Z=0.05m

Table2: Break Frequency Values and Resonance Under Influence of the Radiation Thermal Exchange Coefficient

	radiation thermal exchange coefficient (W.m ⁻² .K ⁻¹)			
	100	90	80	70
Break frequency (rad/s)	10 ^{-2.881}	10 ^{-2.874}	10 ^{-2.868}	10 ^{-2.862}
	10 ^{-2.840}	10 ^{-2.837}	10 ^{-2.831}	10 ^{-2.826}
Resonance frequency (rad/s)	10 ^{-2.862}	10 ^{-2.855}	10 ^{-2.849}	10 ^{-2.843}
Ze _{max} (K.m ² .W ⁻¹)	10.833	9.689	7.711	6.400

Table3:Break Frequency Values and Resonance For Different Value of Convection Thermal Exchange Coefficient

	convection thermal exchange coefficient (W.m ⁻² .K ⁻¹)			
	100	90	80	70
Break frequency (rad/s)	10 ^{-3.371}	10 ^{-3.371}	10 ^{-3.371}	10 ^{-3.371}
	10 ^{-2.926}	10 ^{-2.936}	10 ^{-2.954}	10 ^{-2.971}
Resonance frequency (rad/s)	10 ^{-2.926}	10 ^{-2.936}	10 ^{-2.954}	10 ^{-2.971}
Ze _{max} (K.m ² .W ⁻¹)	0.299	0.274	0.249	0.222

B. Bode Diagramm of the Equivalent Impedance Phase

Figures 5 and 6 allow give conclusion on the thermal behavior of bearing layer. We notice a frequency band in whichn, the thermal impedance phase is positive showing the predominance of inductive effect. For these frequency the amount of heat received by the bearing layer is dissipated through the other layers.

For the negative values of frequency in which the phase is negative, (predominance of capacitive effects), the bearing layer restore the heat flow. The values equal to zero are related on the resonance.

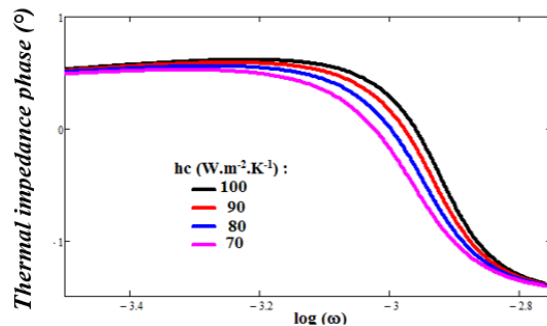


Figure 6: Equivalent Thermal Impedance Phase According to the Decimal Logarithm of the Pulse.
Hc=0.01W.M⁻².K⁻¹, I=800W.M⁻², Z=0.05m

C. Nyquist Representation of the Equivalent Thermal Impedance

The NYQUIST representation confirms results got from Bode diagram and the phase [34]. It permits to validate the stability of a system. In illumination zone, thermal impedance curves present both the capacitive and inductive predominance. These two phenomena are separated by the resonance. For this weather condition, the bearing layer reaches its thermal stability.

The frequency limit values allow having the thermoelectric parameter in the corresponding layer. Indeed, the shunt resistance corresponds to the double of the imaginary part maximum of the thermal impedance. For the parallel resistance, it corresponds to the real part when the imaginary part is equal to zero.

In shadowed zone, the series resistance is added to the preceding parameters, translating heat losses in the layer by restitution.

Tables 4 and 5 give the resistance values in the two zone.

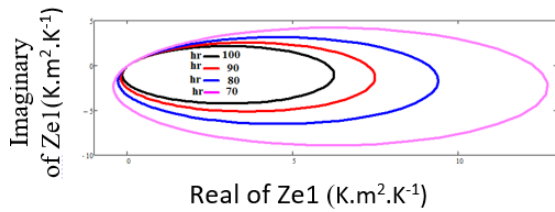


Figure 7: Thermal Impedance Imaginary Part According to the Real Part Under Influence of the Radiation Thermal Exchange Coefficient. $H_c=0.01\text{W}\cdot\text{M}^{-2}\cdot\text{K}^{-1}$, $I=800\text{W}\cdot\text{M}^{-2}$, $Z=0.05\text{m}$

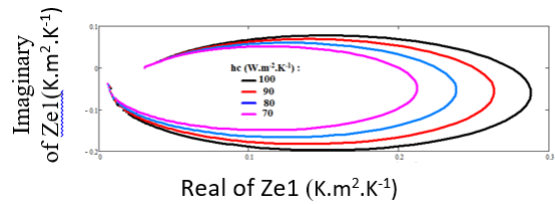


Figure 8: Thermal Impedance Imaginary Part According to the Real Part Under Influence of the Convection Thermal Exchange Coefficient. $H_r=0.01\text{W}\cdot\text{M}^{-2}\cdot\text{K}^{-1}$, $I=800\text{W}\cdot\text{M}^{-2}$, $Z=0.05\text{m}$

Table 4: Parallel and Shunt Resistance Under Influence of Radiation Thermal Exchange Coefficient

	radiation thermal exchange coefficient ($\text{W}\cdot\text{m}^{-2}\cdot\text{K}^{-1}$)			
	100	90	80	70
Parallel resistance ($\text{K}\cdot\text{m}^2\cdot\text{K}^{-1}$)	6.15	7.21	9.14	12.21
Shunt resistance ($\text{K}\cdot\text{m}^2\cdot\text{K}^{-1}$)	4.26	5.06	6.28	8.38

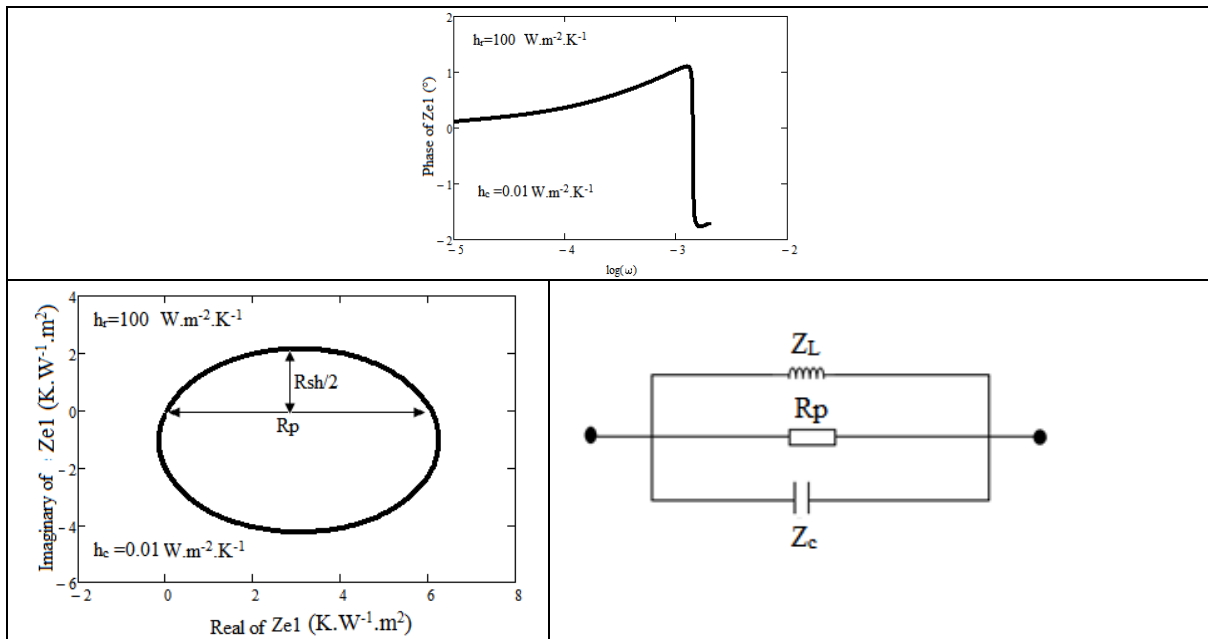
Table5: Resistances Parallel, Shunt and seriefor Different Value of convection Thermal Exchange Coefficient

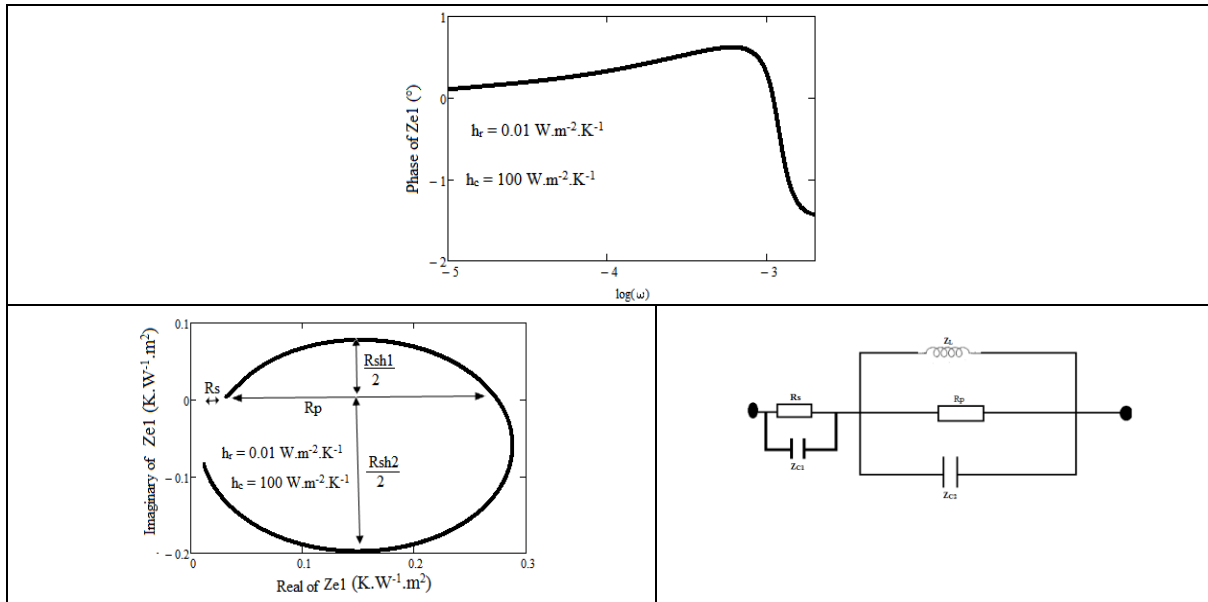
	Convection thermal exchange coefficient ($\text{W}\cdot\text{m}^{-2}\cdot\text{K}^{-1}$)			
	100	90	80	70
Parallel resistance ($\text{K}\cdot\text{m}^2\cdot\text{K}^{-1}$)	0.240	0.220	0.190	0.170
Shunt resistance ($\text{K}\cdot\text{m}^2\cdot\text{K}^{-1}$)	0.154	0.136	0.118	0.102
Series resistance ($\text{K}\cdot\text{m}^2\cdot\text{K}^{-1}$)	0.02	0.02	0.02	0.02

D. Equivalent Electric Model

The equivalent electric circuit of the model is proposed by the two conditions:

- Equivalent electric model of the road in illuminated zone
- Equivalent electric model of the road in shadowed zone





CONCLUSION

The thermal behavior modeling of the bearing road body has been done under illumination and shade. The thermal impedance spectroscopy study from Bode diagram, the phase and the NYQUIST representation has helped determining the break frequency, the resonance frequency ant series, shunt, parallel resistances.

The representation has allowed introducing equivalent electric models and giving conclusion relating on the bearing layer thermal stability.

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