

# Optimal Control Scheme for Non-Quadratic Performance Based on DHP Algorithm in Neural Networks

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## Abstract

*In this paper, an efficient method has been proposed for transmission line over load alleviation in deregulated power system. Here the generators are selected based on their sensitivity to the congested line and the active power of the participating generators are rescheduled using the bacterial foraging algorithm along with fuzzy for relieving congestion. The algorithm is tested in IEEE 30-bus system and compared with the simple bacterial foraging and particle swarm optimization for its effectiveness and robustness in congestion management. It is observed that the bacterial foraging algorithm (BFA) with fuzzy minimizes the cost effectively when compared to the simple bacterial foraging (SBF) and particle swarm optimization (PSO).*

**Keywords**—Congestion management, Deregulated market, SBF, PSO, Generator Sensitivity, Constraints

## I. INTRODUCTION

Bacteria Foraging Optimization Algorithm (BFOA), proposed by Passino [16], is a new comer to the family of nature-inspired optimization algorithms. In competitive markets, electricity price is regulated based on proposals offered by all market participant, these markets provide the possibility of exchanging energy between various participants. Electricity is a commodity with special features which should be considered when making laws. For example, it is difficult to save, in any case it has losses when transmitting and controlling the electricity flow requires using expensive equipment. Congestion is defined as the overloading of one or more transmission lines and/or transformers in the power system. In the deregulated electricity market, congestion occurs when the transmission system is unable to accommodate all of their desired transactions due to violation of MVA limits of transmission lines. In such market, most of the time, the transmission lines operate near to their stability limits as all market players try to maximize their profits from various transactions by fully utilizing transmission systems.

R.D. Christie et al. [1] explained in detail the congestion management and felt that controlling the transmission system so that transfer limits are observed is perhaps the fundamental transmission management problem. In order to relieve congestion, one can either use FACTS devices [2], operate taps of a transformer, redispatch of generation [3] and curtailment of pool loads and/or bilateral contracts. In a deregulated environment, all the GENCOs and DISCOs plan their transactions ahead of time. But by the time

of implementation of transactions there may be congestion in some of the transmission lines. Hence, ISO has to relieve the congestion so that the system remains in secure state. ISO use mainly two types of techniques to relieve congestion and they are as follows:

i) Cost free means:

a. Out-aging of congested lines.

b. Operation of transformer taps/phase shifters.

c. Operation of FACTS [2] devices particularly series devices.

ii) Non-cost free means:

a. Re-dispatch of generation [3] in a manner different from the natural settling point of the market. Some generators backdown while others increase their output. The effect of this is that generators no longer operate at equal incremental costs.

b. Curtailment of loads and the exercise of (non-cost-free) load interruption options.

R.S. Fang et al. [4] considered an open transmission dispatch environment in which pool and bilateral/multilateral dispatches coexist and proceeded to develop a congestion management strategy for this scenario. K.L. Lo et al. [5] presented congestion management techniques applied to various kinds of electricity markets. Ashwani Kumar et al. [6] reviewed extensively the literature for reporting several techniques of congestion management and informed that the congestion management is one of the major tasks performed by Independent System Operators (ISOs) to ensure the operation of transmission system within operating limits. In the emerging electric power markets, the congestion management becomes extremely important and it can impose a barrier to the electricity trading. Ashwani Kumar et al. [7] proposed an efficient zonal congestion management approach using real and reactive power rescheduling based on AC Transmission Congestion Distribution factors considering optimal allocation of reactive power resources. The impact of optimal rescheduling of generators and capacitors has been demonstrated in congestion management. H.Y. Yamina and Shahidehpour [8] described a coordinating mechanism between generating companies and system operator for congestion management using Benders cuts. F. Capitanescu and Van Cutsem [9] proposed two approaches for a unified management of congestions due to voltage instability and thermal overload in a deregulated environment. J. Fu and Lamont [10] discussed a combined framework for service identification and congestion management while a new approach were applied to identify the services of reactive support and real power loss for managing congestion using the upper bound cost minimization.

J. Kennedy and Eberhart [11] described the Particle Swarm Optimization (PSO) concept in terms of its precursors, briefly reviewing the stages of its development from social simulation to optimizer and discussed application of the algorithm to the training of artificial neural network weights. Y. Shi [12] surveyed the research and development of PSO in five categories viz. algorithms, topology, parameters, hybrid PSO algorithms and applications. In general, the search process of a PSO algorithm should be a process consisted of both contraction and expansion so that it could have the ability to escape from local minima, and eventually find good enough solutions.

Y. Del Valle et al. [13] presented a detailed review of the PSO technique, the basic concepts and different structures and variants, as well as its applications to power system optimization problems. Z.X. Chen et al. [14] introduced PSO for solving Optimal Power Flow (OPF) with which congestion management in pool market is practically implemented on IEEE 30 Bus system and proved that congestion relief using PSO is effective in comparison with Interior Point Method and Genetic Algorithm approach. J. Hazra and Sinha [15] proposed cost efficient generation rescheduling and/or load shedding approach for congestion management in transmission grids using Multi Objective Particle Swarm Optimization (MOPSO) method. K.M. Passino [16] explained in detail the biology and physics underlying the chemotactic (foraging) behaviour of *Escherichia coli* bacteria that formulated Simple Bacterial Foraging (SBF) Optimization Algorithm for optimization process represented by the activity of social bacterial foraging. The algorithm presented in [16] has been utilized in this paper for optimal generation of active power of the participating generator.

Fuzzy logic rules is created using fuzzy toolbox of MATLAB to fuzzify the run length vector  $C(i)$  for optimal value which is incorporated in the SBF algorithm. Janardan Nanda et al. [17] made a maiden attempt to examine and highlight the effective application of Bacterial Foraging algorithm to optimize several important parameters in Multiarea Automatic Generation Control (AGC) of a thermal system and compared its performance to establish its superiority over Genetic Algorithm (GA) & classical methods. H. Vahedi et al. [18] proposed a novel Mixed Integer SBF algorithm for solving constrained OPF problem for practical applications. Results show that the Mixed Integer SBF algorithm is superior to PSO based algorithm in terms of solution quality, convergence rate and evolutionary computing time.

It is observed that researchers have not attempted so far to dynamically adjust the run length vector of the SBF algorithm for optimal rescheduling of the active powers of the participating generators by applying fuzzy criterion to relieve congestion in the congested line. Further, no attempt has been made so far to employ SBF for optimal rescheduling of active power of the select participating generators to relieve congestion in the congested line. To incorporate the

innovativeness into congestion management, a new method of BFA with fuzzy is attempted for the first time to relieve congestion in the congested line by optimal rescheduling of active powers of the select participating generators. Instead of selecting all the generators to relieve congestion, in this paper it is proposed to select only those generators which are very sensitive for relieving congestion in transmission lines. This is done by the selection of participating generators using generators sensitivities to the power flow on congested lines. Further, it is proposed to solve congestion management problem by optimal rescheduling of active power of participating generators employing the BFA with fuzzy. Subsequently, the BFA with fuzzy is compared with SBF and conventional PSO algorithm to determine the best optimal solution for rescheduling the active power of participating generators to relieve the congestion.

In this paper static congestion management by optimal rescheduling of active power of the generators selected based on their sensitivities to the congested line is attempted by BFA with fuzzy for the first time and compared the test results with SBF and conventional PSO. The main advantage of this approach of relieving congestion in the congested line is quite efficient as it is a non-cost free mean technique. This paper illustrates the effectiveness of the proposed method on the congestion management problem considering IEEE 30-bus system.

## II. CONGESTION MANAGEMENT METHOD

Congestion is defined as the overloading of one or more transmission lines and/or transformers in the power system. In the deregulated electricity market, congestion occurs when the transmission system is unable to accommodate all of their desired transactions due to violation of MVA limits of transmission lines.

Congestion may lead to rise in cost of electricity, tripping of overloaded lines and consequential tripping of other healthy lines. It may also create voltage stability related problems. It should be relieved to maintain power system stability and security, failing which results into system blackout with heavy loss of revenue. Various factors and phenomena cause congestion on transmission lines that inherent limitations of transmission network can be pointed as one of them which are divided into two major categories:

1. Physical limitations
2. System limitations

Thermal limitation of a transmission line or a transformer is among physical limitations of transmission network. Voltage limitation in a node, transient stability, dynamic stability, reliability and similar cases are also examples of system limitations of transmission network. Given the above limitations, many factors can be effective in the occurrence of congestion on transmission lines, such as energy consumption increase in point in the network, concurrent use of electrical appliances during peak hours and non-coordinated exchanges. Also the departure of a number of transmission lines or power generation units in a point in the network due to error or repairs

makes more loading of network healthy lines and congestion on these lines. Hence, ISO has to relieve the congestion so that the system remains in a secure state. ISO mainly uses two types of techniques to relieve congestion. These are listed below.

- i) Cost free means
  - a. Out-aging of congested lines
  - b. Operation of transformer taps/phase shifters
  - c. Operation of FACTS [2] devices, particularly series devices
- ii) Non-Cost free means
  - a. Re-dispatching power generation [3] in a manner different from the natural settling point of the market. Some generators back down, while others increase their output. Consequently, generators no longer operate at equal incremental costs.
  - b. Curtailment of loads and the exercise of (non-cost free) load interruption options.

### III. BACTERIAL FORAGING WITH FUZZY METHOD

Bacterial foraging algorithm for optimization has been widely accepted as a global optimization algorithm of current interest for distributed optimization and control. Bacterial Foraging Algorithm is inspired by the social foraging behaviour of *Escherichia coli*. This algorithm has already drawn the attention of researchers because of its efficiency in solving real-world optimization problems arising in several application domains.

In a natural evolutionary process the survival of the species depends upon the fitness criteria that is based on the food searching ability and the motile behaviour. The species with better food searching ability tends to move on to the next generation and the species with the poor search ability gets eliminated or gets reshaped to transform into a strong species. The *E. coli* bacteria is generally present in human intestine tends to perform four processes, they are Chemotaxis, Swarming, Reproduction and Elimination-Dispersal event.

**Chemotaxis:** The characteristics of movement of bacteria in search of food can be defined in two ways, i.e. swimming and tumbling together known as chemotaxis. A bacterium is said to be swimming if it moves in a predefined direction, and tumbling if moving in an altogether different direction. Mathematically, tumble of any bacterium can be represented by a unit length of random direction  $\Delta(i)$  multiplied by a step length of that bacterium  $C(i)$ . In case of swimming this random length is predefined.

There is a scope to fuzzify the variable  $C(i)$  for arriving at the optimum value of the step size for the given problem in less time. Initially the run length vector  $C(i)$  value is selected by random selection and it plays an important role in the convergence of SBF algorithm. A small value of  $C(i)$  causes slow convergence, whereas a large value may fail to locate the minima by swimming through them without stopping. The selection of  $C(i)$  is tedious and time-consuming in SBF. Hence, fuzzy adaptive scheme is utilized to  $C(i)$  for ensuring the convergence of SBF algorithm. Here, the fuzzy input variables

are taken as  $C(i)$  and the error from the objective function to obtain the fuzzy output as  $\Delta C(i)$  for optimal value. The fuzzy toolbox of MATLAB package on Windows environment is employed to fuzzify the run length vector  $C(i)$  and the procedure to create fuzzy logic rules using fuzzy logic toolbox is detailed in Appendix A.

**Swarming:** For the bacteria to reach at the richest food location (i.e. for the algorithm to converge at the solution point), it is desired that the optimum bacterium till a point of time in the search period should try to attract other bacteria so that together they converge at the solution point more rapidly. To achieve this, a penalty function based upon the relative distances of each bacterium from the fittest bacterium till that search duration, is added to the original cost function. Finally, when all the bacteria have merged into the solution point this penalty function becomes zero. The effect of swarming is to make the bacteria congregate into groups and move as concentric patterns with high bacterial density.

**Reproduction:** The original set of bacteria, after getting evolved through several chemotactic stages reach the reproduction stage. Here, the best set of bacteria (chosen out of all the chemotactic stages) gets divided into two groups. The healthier half replaces the other half of bacteria, which gets eliminated, owing to their poorer foraging abilities. This makes the population of bacteria constant in the evolution process. The survival and elimination behaviour of any bacterium is better known as its motile behaviour.

**Elimination and dispersal:** In the evolution process a sudden unforeseen event can occur, which may drastically alter the smooth process of evolution and cause the elimination of the set of bacteria and/or disperse them to a new environment. Most ironically, instead of disturbing the usual chemotactic growth of the set of bacteria, this unknown event may place a newer set of bacteria nearer to the food location. From a broad perspective, elimination and dispersal are parts of the population level long distance motile behaviour. In its application to optimization it helps in reducing the behaviour of stagnation (i.e. being trapped in a premature solution point or local optima) often seen in such parallel search algorithms.

Bacterial Foraging Algorithm with Fuzzy for congestion management by optimal rescheduling of generators is as described below:

**STEP 1:** Initialize parameters  $S, N_s, N_c, N_{re}, N_{ed}, P_{ed}, C(i) (i=1, 2, \dots, S), \theta^l$ .

**STEP 2:** Elimination-dispersal loop:  $l = l + 1$ .

**STEP 3:** Reproduction loop:  $k = k + 1$ .

**STEP 4:** Chemotaxis loop:  $j = j + 1$ .

- a) For  $i=1, 2, \dots, S$  to take a chemotactic step for bacterium  $i$
- b) Compute fitness function  $J_{error}(i, j, k, l)$

$$J_{\text{error}}(i,j,k,l) = J_{\text{error}}(i,j,k,l) + J_{\text{cc}}(\theta^i(j,k,l), P(i,j,l))$$

c)  $J_{\text{last}} = J_{\text{error}}(i,j,k,l)$  to save this to find a better cost.

d) Tumble:

Generate a random vector  $\Delta(i) \in R^p$  with each element  $\Delta_m(i)$ , where

$m = 1, 2, \dots, p$ , a random number on  $[-1, 1]$ .

e) move:  $\theta^i(j+1,k,l) = \theta^i(j,k,l) + C(i) \frac{\Delta(i)}{\sqrt{\Delta^T(i)\Delta(i)}}$ , step size  $C(i)$  for bacterium  $i$ . Fuzzify the variable  $C(i)$  using MATLAB Fuzzy toolbox.

f) Compute  $J_{\text{error}}(i,j+1,k,l)$

$$J_{\text{error}}(i,j+1,k,l) = J_{\text{error}}(i,j+1,k,l) + J_{\text{cc}}(\theta^i(j+1,k,l), P(j+1,k,l))$$

g) Swim

1.  $m=0$  represents counter for swim length

2. While  $m < N_s$ ,  $m=m+1$ , If  $J_{\text{error}}(i,j+1,k,l) < J_{\text{last}}$ , if doing better

Let  $J_{\text{last}} = J_{\text{error}}(i,j+1,k,l)$  and

$$\text{Let } \theta^i(j+1,k,l) = \theta^i(j+1,k,l) + C(i) \frac{\Delta(i)}{\sqrt{\Delta^T(i)\Delta(i)}}$$

$$J_{\text{error}}(i,j+1,k,l) = J_{\text{error}}(i,j+1,k,l) + J_{\text{cc}}(\theta^i(j+1,k,l), P(j+1,k,l))$$

Else,  $m=N_s$  and End of while statement

h) Go to next bacterium ( $i + 1$ ), if  $i \neq S$  Go to [b] to process the next bacterium

**STEP 5:** If  $j < N_c$ , Go to 4 to continue chemotaxis, since the life of the bacteria is not over.

**STEP 6:** Reproduction: For the given  $k$  and  $l$ , and for each  $i = 1, 2, \dots, S$ ,

$$J_{\text{health}}^i = \sum_{j=1}^{N_c} J_{\text{error}}(i,j,k,l)$$

**STEP 7:** If  $k < N_{re}$ , Go to 3 to perform reproduction

**STEP 8:** Elimination-dispersal: For  $i = 1, 2, \dots, S$ , with probability  $P_{ed}$ , Perform elimination dispersal to eliminate and disperse one to a random location. If  $1 < N_{ed}$ , Go to 2 Otherwise end.

#### IV. GENERATOR SENSITIVITY

A change in real power flow in a transmission line  $k$  connected between bus  $i$  and bus  $j$  due to change in power generation by generator 'g' can be termed as generator sensitivity to congested line (GS).

$$GS_g = \frac{\Delta P_{ij}}{\Delta P_g}(1)$$

Where,

$\Delta P_{ij}$  = change in the real power flow of the congested line

$\Delta P_g$  = change in the real power generated by the generator

#### V. OBJECTIVE FUNCTION

The objective function of rescheduling real power generation using cost

Minimization is given by

$$C = \text{minimize } \sum_{g=1}^{N_g} C_g(\Delta P_g) \Delta P_g(2)$$

Where

$C_g(\Delta P_g)$  = incremental and decremental bids submitted by generators

$\Delta P_g$  = Unit change in real power adjustment at generator

$N_g$  = Number of generators

Subject to

$$\sum_{g=1}^{N_g} ((GS_g) \Delta P_g) + PF_k^0 \leq PF_k^{\text{max}} \quad (3)$$

Where  $k=1, 2, 3 \dots N_l$

$$\Delta P_g^{\text{min}} \leq \Delta P_g \leq \Delta P_g^{\text{max}} \quad (4)$$

$$\Delta P_g^{\text{min}} = P_g - P_g^{\text{min}} \quad (5)$$

$$\Delta P_g^{\text{max}} = P_g^{\text{max}} - P_g \quad (6)$$

$$\sum_{g=1}^{N_g} \Delta P_g = 0 \quad (7)$$

Where  $g = 1, 2 \dots N_g$

$PF_k^0$  = power flow caused by all contracts requesting the transmission services.

$PF_k^{\text{max}}$  = line flow limit of the line connecting bus- $i$  and bus  $j$

$N_l$  = number of transmission lines in the system.

$GS_g$  = generator sensitivity of generator  $g$ .

#### V. PARAMETER SELECTION AND FUZZY RULES

1) If input is NB, then output is NB.

2) If input is NS, then output is NM.

3) If input is Z, then output is NS.

4) If input is PS, then output is Z.

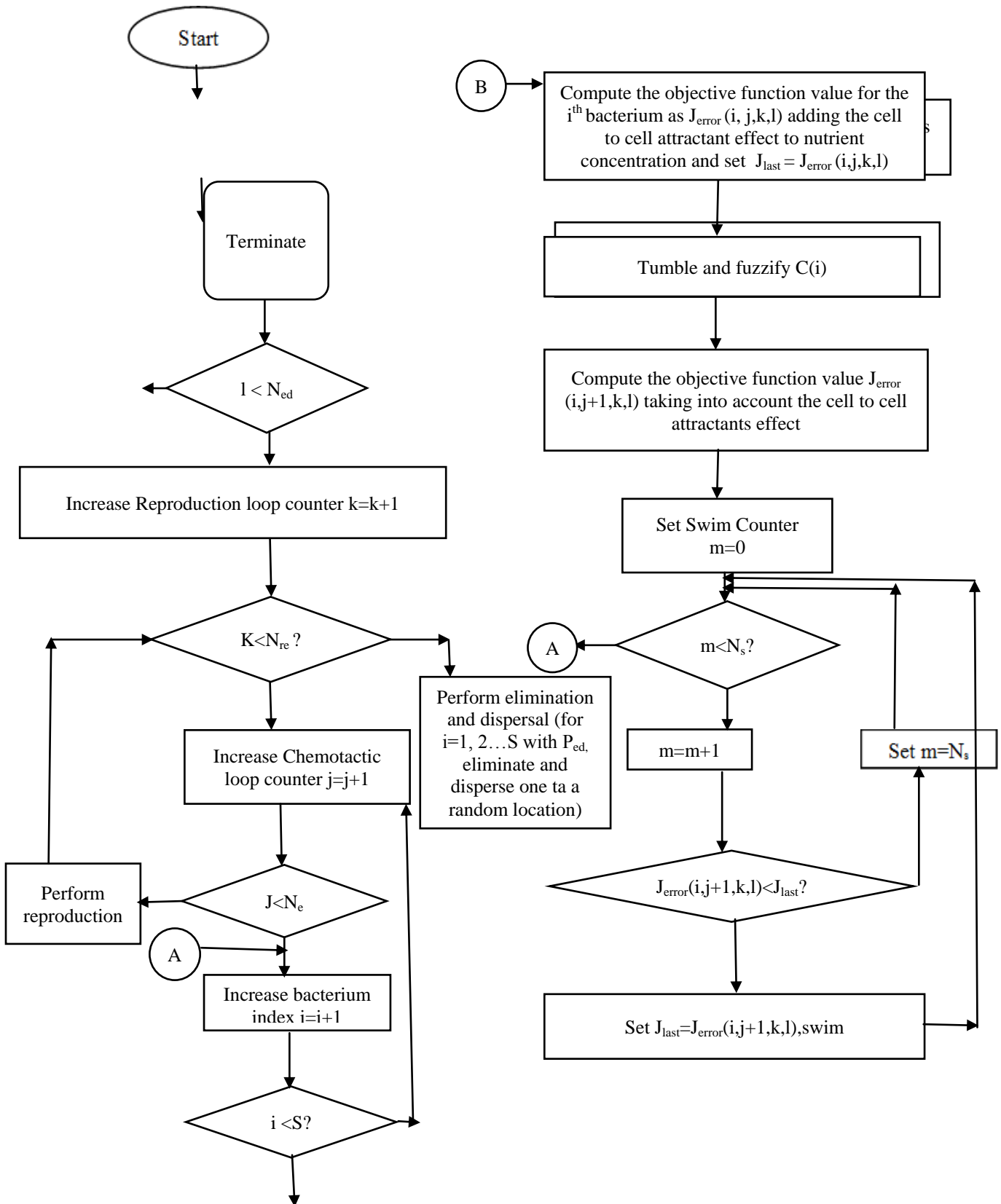
5) If input is NM, then output is PS.

6) If input is PM, then output is PM.

7) If input is PB, then output is PB.

B

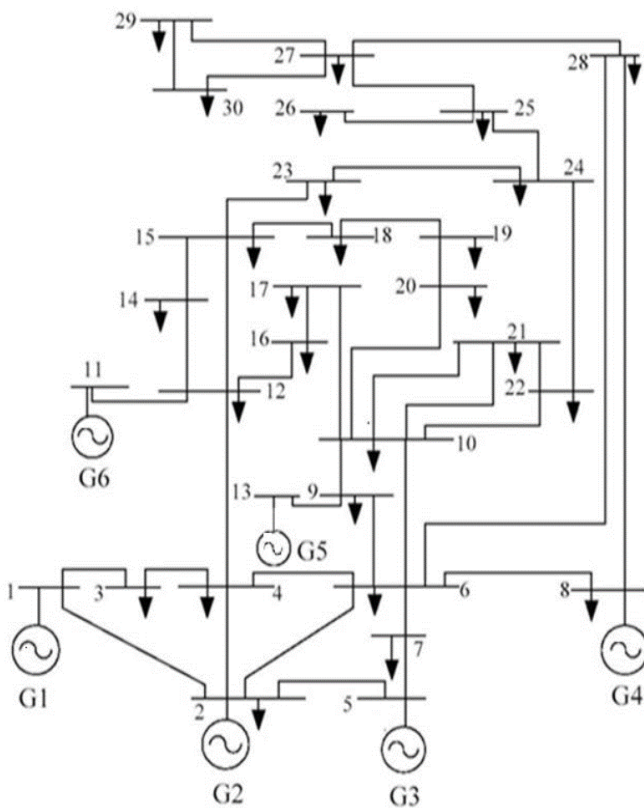
Fig.1.Flowchart of Bacterial Foraging Algorithm



The parameters selected for the proposed bacterial foraging algorithm with fuzzy is as follows:

- Number of bacteria to be optimized, P = 2
- Number of bacteria, S = 30
- Number of chemotactic steps, Nc = 50
- Swimming length, Ns = 4
- Number of reproduction steps, Nre = 4
- Number of elimination & dispersal events, Ned = 2
- Run length vector initial value, C(i) = 0.05
- Probability of elimination & dispersal, Ped = 0.25
- Number of bacteria reproduction, Sr = S/2

**VI. RESULT AND DISCUSSION**



**Fig.2. Single Line Diagram of IEEE 30 Bus System**

The IEEE 30-bus system consists of six generator buses and 24 load buses. Accordingly, the Generator Sensitivities are computed for the congested Line-26 for the system. Generators which are to participate in congestion management are to be selected depending on their sensitivities to the congested line.

In this test system, it is observed that all the generators show strong influence on the congested line. This is perhaps the system is very small and generally very tightly connected electrically. All the generators are participating in congestion management and the evolutionary algorithms are employed to optimally reschedule the active power of the generators for relieving congestion in Line-26. Mostly, congestion is due to exceeding power flow limit of one or more lines and outage of some important elements.

**Table I : Active power flow in congested line after and before congestion management for IEEE 30-bus system**

Branch power flow		Before Congestion management active power flow(MW)	After congestion management active power flow (MW)
From bus	To bus		
10	17	8.4200	8.1260

**Table II : Comparisons of cost of congestion management for IEEE 30-bus system**

Cost of CM(Rs/MWh)	FABF	SBF	PSO
Best	117.4467	177.12	160.23
Mean	134.5100	177.36	161.49
Worst	183.6439	177.38	161.61

**Table III : Active power generation before and after congestion management for IEEE 30-bus system**

Bus no.	Before Congestion management active power generation (MW)	After Congestion management active power generation (MW)
1	188.60	198.5
2	42.40	52.3
5	18.30	28.2
8	10.60	20.51
11	10.80	20.7
13	12.70	22.6

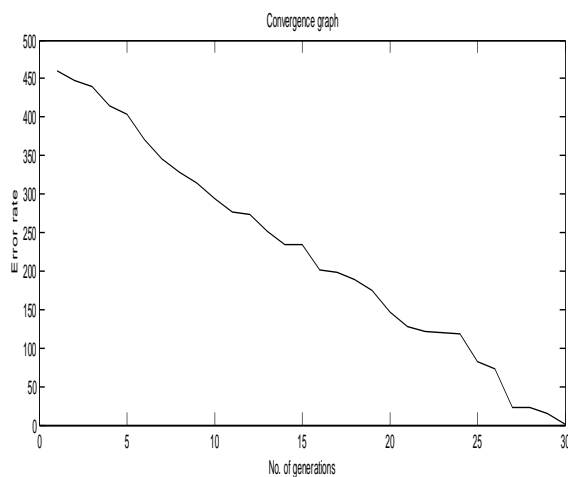


Fig.3. Plot of convergence graph

It has been observed from table I that the transmission line connecting bus 10 and bus 17 carries 8.42 MW power before congestion management. This congestion is created by increasing the load of bus 14. After solving the congestion management problem the power flow in the line 26 is reduced by 8.1260 MW.

From the comparison of the cost of congestion we can conclude that the bacterial foraging algorithm with fuzzy is lowest than the simple bacterial foraging and particle swarm optimization (table II). Fig.3 indicates that the bacterial foraging algorithm with fuzzy converges faster.

## VII. CONCLUSION

Congestion management problem has been solved using optimal rescheduling of active powers of generators selected based on the generator sensitivity to the congested line, utilizing bacterial foraging algorithm with fuzzy. Here rescheduling is done taking into consideration the minimization of cost and satisfying line flow limits. The results obtained by the bacterial foraging with fuzzy are compared with Simple Bacterial Foraging (SBF) and conventional PSO algorithms. This method is tested on IEEE 30-bus. The results show that bacterial foraging algorithm with fuzzy is giving the best optimal solution in comparison with Simple Bacterial Foraging (SBF) and conventional PSO algorithms with respect to cost and runtime for relieving congestion in the congested line.

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