

Computation of material parameters of Chaboche kinematic hardening model using grey wolf optimization and uniaxial ratcheting prediction of SS316 Stainless Steel

Jagabandhu Shit*

Department of Mechanical Engineering, Ram Krishna Mahato Government Engineering College, Purulia, West Bengal, India

Abstract: This paper deals with the computation of hardening parameters using the Grey wolf optimization (GWO) approach with finite element (FE) simulation to study the uniaxial ratcheting behavior of SS316 stainless steel. Chaboche's kinematic hardening model is used to predict this kind of cyclic plastic phenomenon of the material. Ratcheting strain occurs even after the saturation of the material. The parameters obtained from a strain-controlled saturated hysteresis loop are used in the material model. The material model is a plugged infinite element commercial package, ABAQUS, for simulation of ratcheting behavior. The finite element simulation is based on the Von-Mises yield function, flow rule, kinematic hardening rule, and yield surface consistency condition. The proposed optimization technique, GWO, is used for material parameters optimization of SS 316 steel. The simulation results are compared to the one obtained using manually determined parameters. The simulation results confirm the potentiality and efficacy of the proposed KHA method.

Keywords: hardening parameters, Grey wolf optimization, Finite element, ratcheting, Von-Mises yield function.

I. Introduction

In structural components design, mechanical behavior modeling of material is very important to estimate the fatigue life. The mechanical behaviors of materials are modeled initially by the linear Prager [1] model. Subsequently, the advanced plasticity models are proposed by Armstrong and Frederick [2], Chaboche [3], Ohno, and Wang [4] and others.

Chaboche model is the segmentation of Armstrong and Frederick's rule to get segment-wise better results. This decomposition better describes the three critical segments of the loading/unloading branch of the saturated hysteresis loop, i.e., initial part with high modulus, transition knee zone, and linear part at high strain range.

Ratcheting is one of the important cyclic plastic phenomena of the material. In ratcheting, the strain accumulation occurs in loading direction when the material is subjected to stress-controlled cyclic loading with non-zero mean stress. For developing the constitutive models for ratcheting, a lot of efforts are found from the contributors like Burlet&Cailletaud [5], Chaboche et al. [6,7], Guionnet [8], Ohno and Wang [9], Hassan and Kyriakides [10,11], Delobelle et al. [12], McDowell [13], Jiang and Sehitoglu [14], Ohno [15] and others. Above all the Chaboche's model provides a better result for ratcheting simulation. Each model has a large number of material parameters, is determined from different experimental responses. Manual parameter determination for a model is tedious and error-prone. Therefore the optimization technique can be used to automate the optimization of model parameters.

In reference [16-19], genetic algorithm (GA) optimization techniques have been adopted by many researchers for material parameters optimization.

This present work aims to develop a simple and efficient optimization technique to overcome the drawbacks above. Recently, Gandomi [20] proposed a new nature-inspired, population-based meta-heuristic optimization technique, namely krill herd algorithm (KHA), for solving complex numerical problems. The KHA algorithm has excellent exploration and exploitation capabilities, which avoid local optimality and quickly reach the optimal solution.

II. Experimental procedure

A. Uniaxial ratcheting tests

The ratcheting phenomenon is one of the low cycle fatigue responses. The cylindrical fatigue specimen (Figure-1) is used for testing, and the test has been conducted under load-controlled mode. The loading history of the experiment is shown in Figure-2. The tests have been conducted in the universal testing machine(Instron UTM)(Figure-3) with 8810 controllers and a data acquisition system. The ratcheting experiments are conducted at various combinations of



mean stresses and stress amplitudes. Those are m40a310, m60a310, m80a310, m80a270 and m80a350 respectively. The ratcheting load m40a310 implies that mean stress is 40MPa, and stress amplitude is 310 MPa. Figure-4 shows the uniaxial ratcheting response for the ratcheting load m80a350. The ratcheting strain variation with cycles under constant mean stress but

varying amplitudes of stress is shown in Figure-5(a), whereas Figure-5(b) shows the variation of ratcheting strain with cycles under varying degrees mean stresses with constant stress amplitude.

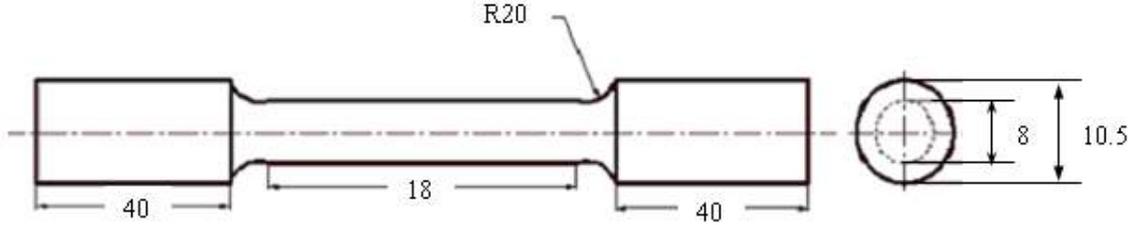


Fig 1: Uniaxial Fatigue Specimen

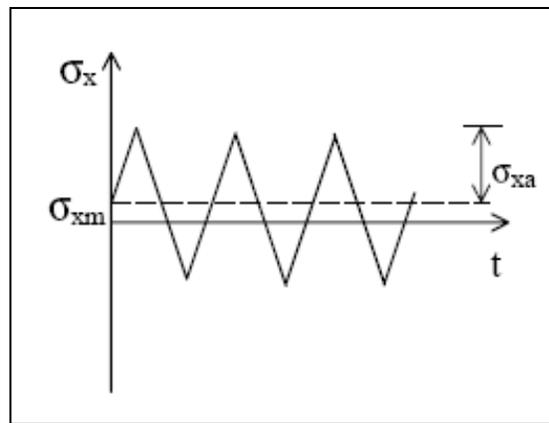


Fig-2: Loading histories; uniaxial stress cycles.



Fig 3: Experimental setup

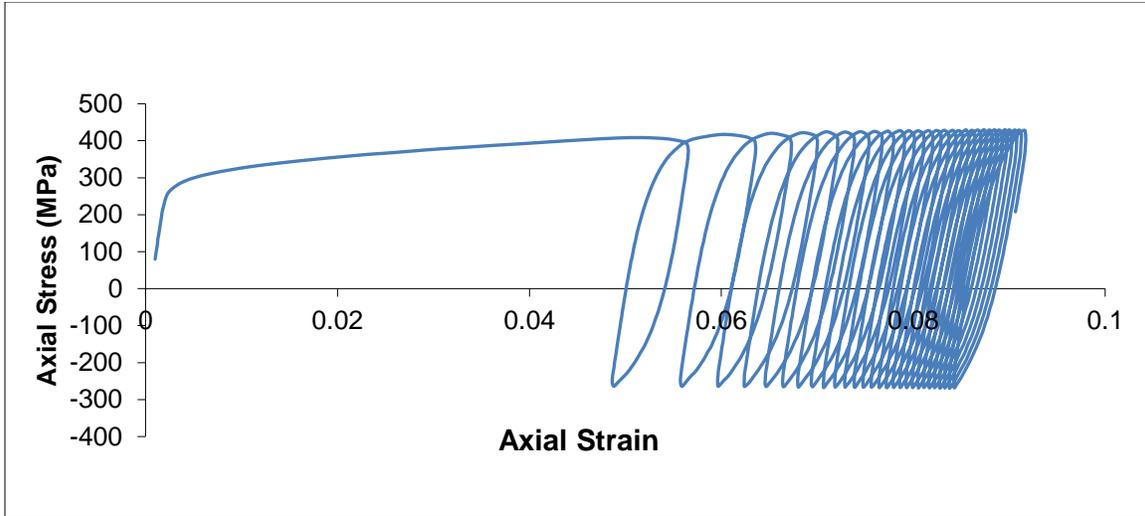


Fig.4: Axial ratcheting strain response for uniaxial stress-controlled cycles with mean stress (ratcheting load m80a350).

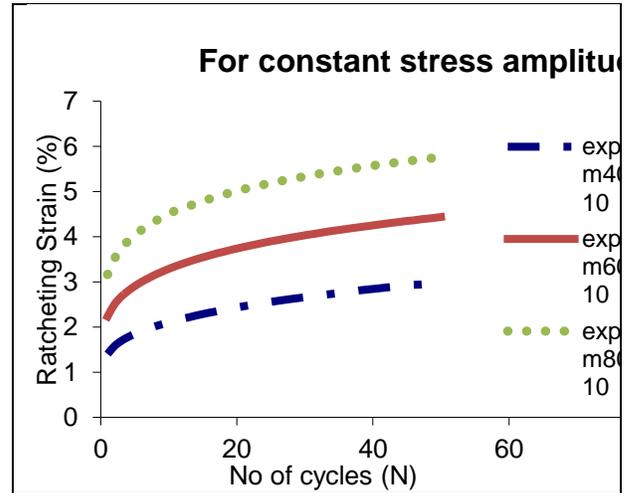
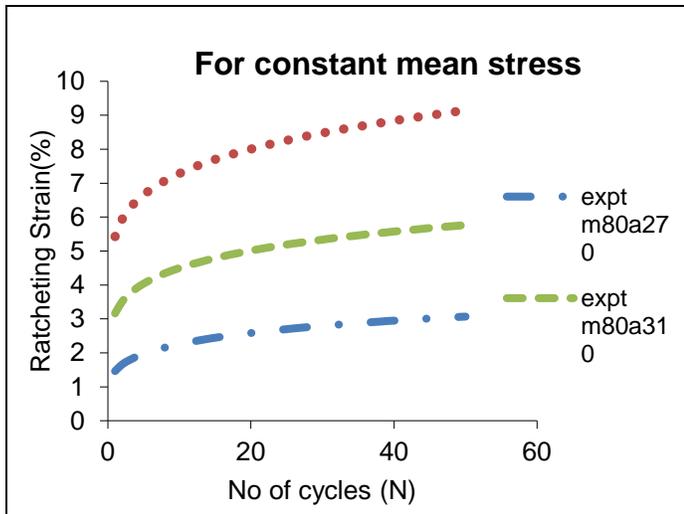


Fig.5:

- (a) Experimental ratcheting strain vs. cycle for constant mean stress.
- (b) Experimental ratcheting strain vs. cycle for constant stress amplitude

III. Cyclic plasticity modeling

The ratcheting behavior of the material is modeled using incremental plasticity theories. The plasticity calculations are based on the yield function, flow rule, hardening rule, and the yield surface's consistency condition. The plastic modulus calculation is coupled with the kinematic hardening rule through the yield surface consistency condition.

$$\text{Von-Mises yield criterion: } \Phi(\bar{\sigma} - \bar{\alpha}) = \left[\frac{3}{2} (\bar{s} - \bar{\alpha})(\bar{s} - \bar{\alpha}) \right]^{1/2} = \sigma_c$$

The stress tensor, the plastic strain tensor, \bar{s} is the deviatoric stress tensor, $\bar{\alpha}$ is the as-back stress tensor, and is the yield surface's size.

Flow Rule:

The Plastic strain rate $\dot{\bar{\epsilon}}^p$ follows from the flow rules as

$$\dot{\bar{\epsilon}}^p = d\epsilon_{eq}^p \frac{\partial \Phi}{\partial \bar{\sigma}}$$

Here $d\epsilon_{eq}^p$ is the equivalent plastic strain rate.

$$d\epsilon_{eq}^p = \left| d\bar{\epsilon}^p \right| = \left[\frac{2}{3} d\bar{\epsilon}^p : d\bar{\epsilon}^p \right]^{1/2}$$

Chaboche kinematic hardening rule.

$$d\bar{\alpha} = \sum_{i=1}^3 d\bar{\alpha}_i, \quad d\bar{\alpha}_i = \frac{2}{3} C_i d\bar{\epsilon}^p - \gamma_i \bar{\alpha}_i d\epsilon_{eq}^p$$

C's, γ 's are model parameters of the Chaboche model.

Consistency condition:

During the plastic deformation, the stress vector remains on the yield surface. This leads to consistency equation, $\dot{\Phi} = 0$

Plastic modulus H is calculated using the consistency condition and is given by the relationship

$$H = \sum_{i=1}^3 H_i$$

Where $H_i = C_i - \gamma_i \left(\bar{\alpha}_i : \frac{\partial f}{\partial \bar{\sigma}} \right)$

Table

Constitutive model parameters determination using manual inspection and GWO for real response

Parameter	Manual calculation	GWO	Parameter	Manual calculation	GWO
$C_{1,i}$ (MPa)	75000	71555	γ_1	1500	1486
C_2 (MPa)	35000	36236	γ_2	348	325
C_3 (MPa)	4000	4569	γ_3	0	0
Fitness Value	Manual calculation			GWO	
Uniaxial ratcheting fitness	0.0958			0.0374	

IV. Finite element simulation of ratcheting behavior

To study materials' ratcheting behavior, the stress-controlled test with non zero mean stress is conducted on a round bar specimen. Chaboche kinematic hardening model has been used for finite element simulation. The GWO optimization procedure has minimized the objective function, and the results are compared with that of the results obtained using a manual procedure. The comparison of experimental results with the simulation result obtained using the

manual procedure and GWO approach for saturated stress-strain loop of $\pm 1.0\%$ strain amplitude using Chaboche's sharpening model is shown in Figure-6. The results obtained using the GWO approach shows better matching with the experimental results than the result obtained using manual calculation procedure.

Figure-7 show the result obtained using Chaboche KH law using both approaches. GWO approach gives a better ratcheting rate than the normal approach for the ratcheting load.

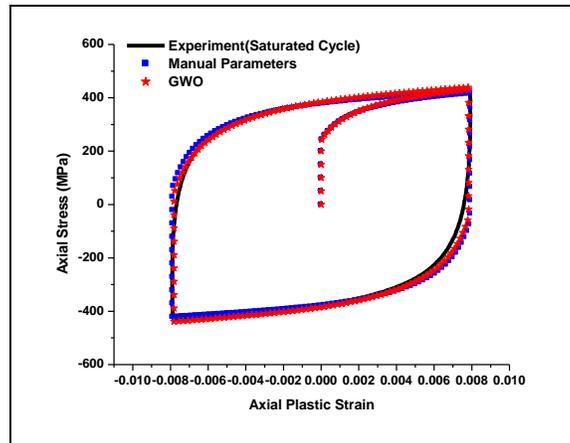


Fig 6 Stable stress-strain hysteresis loop for $\pm 1.0\%$ strain amplitude using Chaboche rule (ABAQUS results).

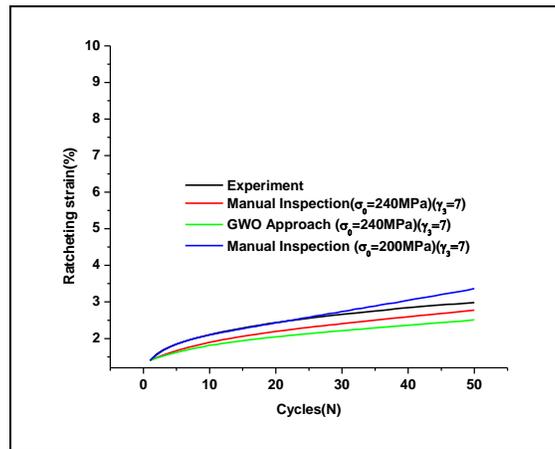


Fig 7: variation of ratcheting strain with cycles for ratcheting load of m40a310.

V. Conclusion

A new meta-heuristics optimization method named Grey wolf optimization (GWO) was developed in this research work to perform material parameter identification of an SS 316 stainless steel. Moreover, stress-controlled low cycle fatigue tests at various combinations of mean stress and amplitude stress are performed to obtain an experimental database on this material. The Chaboche kinematic hardening material model is used to describe material behavior. The simulation results clearly show that the GWO algorithm can fit the experimental behavior. It is also observed that the GWO provides a better ratcheting rate for the case of uniaxial ratcheting in comparison with the manual approach.

References

- [1] W. Prager, "A new method of analyzing stresses and strains in work hardening plastic solids," ASME J. Appl. Mech. 23 (1956) 493-496.
- [2] P. J. Armstrong and C. O. Frederick, "A mathematical representation of the multiaxial Bauschinger effect," GEGB Report RD/B/N (1966) 731-747.
- [3] J. L. Chaboche, "Time-independent constitutive theories for cyclic plasticity," Int. J. Plast., 2 (1986) 149-188.
- [4] N. Ohno and J. D. Wang, "Transformation of a nonlinear kinematic hardening rule to a multi-surface form under isothermal and nonisothermal conditions," Int. J. Plast. 7 (1991) 879-891.
- [5] Burlet, H., Cailletaud, G., 1986. 'Numerical techniques for cyclic plasticity at variable temperature.' Engng. Compt., 3, 143-153.

- [6] Chaboche, J.L., 1991. "On some modifications of kinematic hardening to improve the description of ratcheting effects". *Int. J. Plasticity*, 7, 661-678.
- [7] Chaboche, J.L., 1994. 'Modeling of ratcheting: evaluation of various approaches.' *Eur. J. Mech., A/Solids*, 13, 501-518.
- [8] Guionnet, C., 1992. 'Modeling of ratcheting in biaxial experiments.' *ASME J. Engng. Mater. Techn.*, 114, 56-62.
- [9] Ohno, N., Wang, J.-D., 1993. 'Kinematic hardening rules with critical state of dynamic recovery, part I: formulations and basic features for ratcheting behavior.' *Int. J. Plasticity*, 9, 375-390.
- [10] Hassan, T., and Kyriakides, S. (1994a). 'Ratcheting of Cyclically Hardening and Softening Materials, Part I: Uniaxial Behavior.' *International Journal of Plasticity*, Vol 10, pp. 149-184.
- [11] Hassan, T., and Kyriakides, S. (1994b). 'Ratcheting of Cyclically Hardening and Softening Materials, Part II: Multiaxial Behavior.' *International Journal of Plasticity*, Vol 10, pp. 185-212.
- [12] Delobelle, P., Robinet, P., and Bocher, L. (1995). 'Experimental Study and Phenomenological Modelization of Ratchet Under Uniaxial and Biaxial Loading on an Austenitic Stainless Steel.' *International Journal of Plasticity*, Vol 11, pp. 295-330.
- [13] McDowell, D.L. (1995). 'Stress State Dependence of Cyclic Ratcheting Behavior of Two Rail Steels.' *International Journal of Plasticity*, Vol 11, pp. 397-421.
- [14] Jiang, Y., Sehitoglu, H., 1996a. 'Modeling of cyclic ratcheting plasticity, part I: development of constitutive relations.' *ASME J. App. Mech.*, 63, 720-725.
- [15] Ohno, N. (1997). 'Current State of the Art in Constitutive Modeling for Ratcheting.' *Proceedings of the 14th International Conference on SMiRT*, Lyon, France, pp. 201-212.
- [16] M. Franulovic, R. Basan, I. Prebil, "Genetic algorithm in material model parameters identification for low-cycle fatigue," *Computational Materials Science*, 45 (2) (2009) 505-510.
- [17] A. H. Mahmoudi, S. M. Pezeshki-Najafabadi, H. Badnava, Pezeshki-Najafabadi, and H. Badnava, "Parameter determination of Chaboche kinematic hardening model using a multi-objective Genetic Algorithm," *Computational Materials Science*, 50 (3) (2011) 1114-1122.
- [18] B. M. Chaparro, S. Thuillier, L. F. Menezes, P. Y. Manach, J. V. Fernandes, "Material parameters identification: Gradient-based, genetic and hybrid optimization algorithms," *Computational Materials Science*, 44 (2) (2008) 339-346.
- [19] M. Franulovic, R. Basan, B. Krizan, "Kinematic Hardening Parameters Identification concerning Objective Function," *International Journal of Mechanical, Aerospace, Industrial, Mechatronic and Manufacturing Engineering*, 8 (4) (2014) 685-689.
- [20] A.H. Gandomi, A.H. Alavi, "Communications in Nonlinear Science and Numerical Simulation, Krill herd": A new bio-inspired optimization algorithm, 17 (12) (2012) 4831-4845.