Original Article

Cd_{0.75}Sr_{0.25}F₂: A Potential Dielectric Layer for GaP Based Metal-Insulator-Semiconductor Structures

Alice Bukola Olanipekun¹, Olumide Idowu Akasoro²

¹Department of Physics, Caleb University, Imota, Lagos, Nigeria. ²Department of Physics with Electronic, Lagos State University of Science and Technology, Ikorodu, Lagos, Nigeria.

¹Corresponding Author : bukola.olanipeun@calebuniversity.edu.ng

Received: 13 January 2024 Revised: 25 February 2024 Accepted: 12 March 2024 Published: 27 March 2024

Abstract - $Cd_{0.75}Sr_{0.25}F_2$ is a mixed alloy that has the potential to function as an insulating layer in metal insulator semiconductor (MIS) systems. A theoretical investigation of the structural and dielectric properties of $Cd_{0.75}Sr_{0.25}F_2$ and its binary fluorides (CdF₂ and SrF₂) is reported utilizing the Pseudopotential Plane-Wave (PP-PW) approach in Density Functional Theory (DFT) and Density Functional Pertubation Theory (DFPT). For the exchange-correlation (XC) potentials, this method employs the generalized gradient approximation (GGA). The binary compounds' and alloy's lattice constant, bulk modulus, refractive index, static dielectric constant, band gap, intrinsic breakdown field, energy density, storage density, and lattice misfit are all reported. The estimated lattice constants agreed with the experimental data. The bulk modulus for SrF_2 is consistent with experimental results. The computed bulk modulus of $Cd_{0.75}Sr_{0.25}F_2$ (87.6GPa) shows it is moderately hard. The intrinsic breakdown field depends on the band gap, while the energy storage density depends on the band gap and dielectric constant. A linear relationship is obtained between the intrinsic breakdown field and band gap of considered fluorides and oxides. The intrinsic breakdown field increases in the order HfO_2 — CdF_2 — $Cd_{0.75}Sr_{0.25}F_2$ — SiO_2 — SrF_2 while the energy density increases in the order HfO_2 — SiO_2 — CdF_2 — SrF_2 — $Cd_{0.75}Sr_{0.25}F_2$. The predicted band gap and dielectric constant of $Cd_{0.75}Sr_{0.25}F_2$ are 8.19eV and 8.714, respectively. The intrinsic breakdown field of $Cd_{0.75}Sr_{0.25}F_2$ is 2.78V/nm. Its energy storage density is 299.13J/cm³. There is an improvement in the values of dielectric constant and energy storage density for $Cd_{0.75}Sr_{0.25}F_2$ when compared with SiO₂. These properties of $Cd_{0.75}Sr_{0.25}F_2$ make it a potential insulating layer for MIS devices. From the calculation of lattice mismatch, $Cd_{0.75}Sr_{0.25}F_2$ and CdF_2 have a mismatch of <1%, which makes them suitable dielectric layers on the Gallium Phosphide (GaP) substrate.

Keywords - DFT, DFPT, Dielectric constant, Insulating layer, Intrinsic breakdown field, Energy storage density.

1. Introduction

The discovery of novel materials or the progressive application of existing ones is critical for technological progression in domains such as electronics, optics, engineering, and so on. To prevent extinction due to the overuse of existing materials and to supplement the latter. more materials must be studied to determine their prospective applications. Dielectrics play a crucial role in the operation of Metal-Insulator-Semiconductor (MIS) systems because they serve as insulators and store electric charges. In electronic devices, dielectric materials act as insulation between conductors. An excellent dielectric material has a high breakdown field, as well as resilience to stress, heat, and chemical reactions. The dielectric constant (k) is a measure of a dielectric's ability to store electrical charges. The properties and behavior of dielectric materials must be understood for designing high-quality MIS structures for various electronic applications. MIS devices include MIS capacitors, transistors, memories, charge-coupled devices, deep ultraviolet light emitting diodes, MIS solar cells, field effect diodes, etc.

SiO₂ is a widely used insulating layer due to its insulating properties. It has a band gap of 8.90 and a dielectric constant of 3.9. Its breakdown field is recorded as 2.7V/nm. Due to the scaling down of the thickness of SiO₂ to a few nanometers, the performance of MIS devices has been improved because smaller MIS structures operate faster than larger MIS structures due to high current drive. However, the reduction leads to the problem of leakage current, which results in heating, high power usage, and short-term performance of MIS devices. Since the dielectric constant is inversely proportional to the leakage current, many high k oxides have been proposed to replace SiO₂ to overcome the leakage effects. However, band gap reduces with increasing k, indicating low dielectric strength or breakdown field. The band gaps of most of the proposed materials are relatively low (between 4eV and 6eV) [1] compared with that of SiO₂. Hence, designing MIS structures requires a balance for dielectric constant k, band gap $E_{g_{\text{s}}}$ and intrinsic breakdown field E_{BD} [1]. The insulating dielectric is deposited on a

substrate which is a semiconductor. To maintain interfacial stability between the dielectric layer and the substrate, the difference between the lattice parameters of the dielectric and substrate must be less than 1% for a stable structure.

The alkaline earth fluorides are good materials for insulating layers on semiconductors because they have wide band gaps. They have a fluorite structure, which is similar to the zinc blend or diamond structure of frequently used substrates with good lattice matching.

There are records in the literatures of epitaxial growth of CaF_2 and CdF_2 on Si substrate [2, 3], growth and characterization of SrF_2 on InP substrate [4], the structure of $Ca_xSr_{1-x}F_2$ epilayer on GaAs and Ge substrates [5] and growth characteristics of ultra-thin $Ca_xMg_{1-x}F_2$ alloys on Si substrate [6].

In 2004, Buchinskaya and Fedorov [7] discovered a $Cd_{0.75}Sr_{0.25}F_2$ solid solution to have the fluorite structure after it was formed by the Bridgman Stockbarger method [8]. They found the melting point of the crystal to be 1298K.

The lattice parameter variation with temperature of CdF₂, SrF₂ and Cd_{1-x}Sr_xF₂ (x = 0.23, 0.50) solid solutions was investigated through experiments at 5-300 K [9]. The heat capacity of Cd_{0.50}Sr_{0.50}F₂ was investigated at various temperatures, and structural disorder of the crystal occurred at low temperatures causing the crystal to behave as a glass [10].

The ionic, electrical and thermal conductivities of $Cd_{0.77}Sr_{0.23}F_2$ solid solution have been studied [11]. The crystal has a low thermal conductivity of 1.1W/mK at 300K. As temperature increases, the thermal conductivity of the crystal reduces only slightly [12]. The thermal conductivities of all the compositions of $Ca_{1-x}Sr_xF_2$ ($0 \le x \le 1$) crystal are high (i.e. $\lambda > 3W/mK$ at 300K) [13].

In this work, we would like to study the structural and dielectric properties of CdF_2 , SrF_2 , and $Cd_{0.75}Sr_{0.25}F_2$. The structural properties include the lattice parameter, bulk modulus and lattice mismatch. In contrast, the dielectric properties include the static dielectric constant, the band gap, the intrinsic breakdown field and electrical energy density. The discovery of new insulating layers for MIS structures requires a balance for the dielectric constant, band gap and intrinsic breakdown field [14].

2. Computational Details

The structural characteristics of $Cd_{0.75}Sr_{0.25}F_2$ and its binary fluorides are studied using density functional theory (DFT) with the ultrasoft pseudo-potential, plane wave approach, which is implemented in Quantum Espresso code [15]. The orbitals of Cd (4d¹⁰, 5s²), Sr (4s² 4p⁶ 4d¹⁰, 5s¹), and F (2s² 2p⁵) are treated as valence electrons. Perdew, Burke, and Ernzerhof's exchange-correlation (PBE) [16] is employed. Brillouin zone integration is accomplished using the Monkhorst and Pack meshes [17]. We sampled $6 \times 6 \times 6$ k locations to calculate the alloy's total energy accurately. The kinetic energy cutoff is 60Ryd.

DFT is a well-accepted theory for calculating the physical characteristics of materials. When a system is agitated, specific physical properties are obtained. Examples include an electronic contribution to the dielectric constant, phonon frequencies, Born effective charges, *etc.* These properties are calculated by powerful techniques known as Density Functional Perturbation Theory (DFPT). Most physical properties of solid materials depend on the valence electrons. The valence electron is modeled by the pseudopotential approximation.

The structural properties of the binary compounds CdF_2 and SrF_2 in the fluorite phase are first calculated, followed by $Cd_{0.75}Sr_{0.25}F_2$ using the GGA scheme. For the considered materials, we performed structural optimization by minimizing the total energy with respect to the cell parameters and also the atomic positions. The alloy was studied by using a primitive mesh of 12 atoms. The total energies calculated as a function of cell parameters were fitted to Murnaghan's equation of state [18] to obtain the equilibrium structural properties both for the binary compounds and ternary alloy. The equation of state for energy is given as;

$$E(V) = E_o + \frac{B_o V}{B'_o} \left[\frac{(V_o/V)^{B'_o}}{B'_o - 1} + 1 \right] - \frac{B_o V_o}{B'_o - 1}$$
(1)

The equation of state for pressure is given as;

$$P(V) = \frac{B_o}{B'_o} \left[\left(\frac{V_o}{V} \right)^{B'_o} - 1 \right]$$
(2)

Quantities such as electronic contribution to dielectric constant, Phonon frequencies and Born effective charges that can be obtained by perturbing the total energy are calculated by using DFPT. Here, the total energy is differentiated with respect to the perturbation.

$$E_n = \frac{1}{k!} \frac{d^k E_n}{d\lambda^k} \tag{3}$$

Where E=total energy, n=number of atoms, k=order of perturbation, λ =perturbations, which could be atomic displacement, electric field, etc.

The total or static dielectric constant is divided into electronic contribution and ionic contribution. That is,

$$k = k_e + k_i \tag{4}$$

Where k is the total dielectric constant, k_e is the electronic dielectric constant and k_i is the ionic dielectric constant.

The electronic contribution to the dielectric constant is given as a tensor.

$$k_e = \delta_{\alpha\beta} + 4\pi \frac{\partial P_\alpha}{\partial \varepsilon_\beta} \tag{5}$$

Where α and β are the directions of the electric field (ϵ) and electronic polarization (P).

When $\alpha = \beta$, $\delta_{\alpha\beta} = 1$ and when $\alpha \neq \beta$, $\delta_{\alpha\beta} = 0$.

The refractive index, n, is related to the average k_e by the relation [19]

$$k_e = n^2$$

So that,

$$n = \sqrt{k_e} \tag{6}$$

The band gap energy is related to the refractive index by the Herve-Vandamme relation [20]

$$n^2 = 1 + \left(\frac{A}{E_g + B}\right)^2 \tag{7}$$

Where A=13.6eV, B=3.46eV and $E_{\rm g}$ is the band gap energy.

The relationship between intrinsic breakdown field (E_{BD}) and band gap (E_g) [21] is given as

$$E_{BD} = 1.36 \times \left(\frac{E_g}{E_{gc}}\right)^{\alpha} \tag{8}$$

Where $\alpha = 1$ for insulator, E_{gc} =critical band gap=4eV

Equation (8) can be modified as

$$E_{BD} = \frac{1.36}{4} \times E_g = 0.34 \times E_g$$
 (9)

Born effective charge, Z* is also known as a transverse or dynamic effective charge. It is a basic parameter. Born effective charge is the change in polarization when an atom is displaced or the change in force induced on a given atom when an electric field is applied.

$$Z^* = \Omega_o \frac{\partial P_\beta}{\partial \tau_{\kappa\alpha}(q=0)} = \frac{\partial F_\alpha}{\partial \varepsilon_\beta}$$
(10)

 Ω_{o} =unit cell volume, F_{α} = force on an atom in α direction, P_{β} = polarization in β direction, ε_{β} =electric field in β direction and $\tau_{\kappa\alpha}$ = atomic displacement of atom k in α direction. It is a tensor. The second derivative of the energy with respect to atomic displacement is a $3N \times 3N$ matrix where N is the number of atoms per unit cell. The matrix contains the interatomic force constants whose diagonalization produces phonon frequencies and eigenvectors (displacement).

The ionic contribution to the dielectric constant is given by [22]

$$k_i = \sum \frac{Ne^2 Z^* 2}{m\omega_{TO}^2} \tag{11}$$

N= number of ions per unit volume e= electronic charge Z*= transverse effective charge m= reduced mass ω_{TO}= transverse optical phonon frequency

Another important parameter is the electrical energy storage density [1], which can be used for the appropriate selection of dielectric materials for MIS structures.

$$F_{ED} = 8.1882 \times k \left(\frac{E_g}{E_{gc}}\right)^{2\alpha}$$
(12)

Equation (12) can be modified as

$$F_{ED} = \frac{8.1882}{16} \times kE_g^2 = 0.5118 \times kE_g^2 \tag{13}$$

3. Results and Discussion

3.1. Structural Properties

Table 1 displays the crystals' lattice properties. The lattice parameters for CdF₂, SrF₂, and Cd_{0.75}Sr_{0.25}F₂ are 5.448Å, 5.816Å, and 5.562Å, respectively. They concur with the experiment's findings. The experimental lattice parameters for binary compounds are derived from [23], whereas those for alloys are taken from [7].

Table 1 also includes information on the bulk modulus. Only the experimental bulk modulus of SrF_2 [24] is known, and it is consistent with our results. The bulk moduli of the fluorides are 96.5GPa, 69.1GPa, and 87.6GPa for CdF₂, SrF_2 , and Cd_{0.75} $Sr_{0.25}F_2$, respectively, indicating that they can sustain stress. The bulk modulus of the alloy demonstrates that it is relatively hard, making it suitable as an insulating layer.

Table 1. Lattice constants a(Å) and Bulk modulus B(GPa) of CdF₂, SrF₂ and Cd_{0.75}Sr_{0.25}F₂

Materials	a(Å)	aexp(Å)	B(GPa)	Bexp(GPa)
CdF ₂	5.448	5.388	96.5	
SrF ₂	5.816	5.799	69.1	69.0
Cd _{0.75} Sr _{0.25} F ₂	5.562	5.478	87.6	

3.2. Dielectric Properties

The electronic contribution to the dielectric constant and refractive indices of CdF_2 , SrF_2 and $Cd_{0.75}Sr_{0.25}F_2$ are presented in Table 2. The dielectric constants are 2.778, 2.201 and 2.600, respectively. The value of k_e for SrF_2 compared well with the experiment [25]. The refractive indices of the systems are obtained from (6). The values of n for the binary compounds also compared well with experimental values [25, 26].

Table 2. Electronic contribution to dielectric constant k and refractive indices n of CdF₂, SrF₂ and Cd_{0.75}Sr_{0.25}F₂

Materials	ke	ke (exp)	n	n(exp)
CdF ₂	2.778		1.667	1.66
SrF_2	2.201	2.2106	1.484	1.4868
$Cd_{0.75}Sr_{0.25}F_2$	2.600		1.612	

Table 3 shows the band gap and static dielectric constants of considered materials. For the band gap of $Cd_{0.75}Sr_{0.25}F_2$, we used the Herve-Vandamme relation (7), and the predicted band gap of $Cd_{0.75}Sr_{0.25}F_2$ is 8.19eV. The band gaps of CdF_2 and SrF_2 are experimental values [27, 28]. The static dielectric constants of the materials are also presented in Table 3. For CdF_2 , k=8.827, for SrF_2 , k =6.151 and for $Cd_{0.75}Sr_{0.25}F_2$, k =8.714. The dielectric constants of CdF_2 and SrF_2 compared well with reported values [29, 30]. Since the dielectric constant of SiO_2 , $Cd_{0.75}Sr_{0.25}F_2$, the dielectric layer can be thicker for the same stored charges as shown in Fig.1(a) and Fig. 1(b). The thickness reduces the problem of leakage current which leads to heating, high power consumption and device breakdown.

Table 3. Band gap energies $E_g(eV)$ and static dielectric constants k of

Materials	Eg(eV)	k	k(rep)
CdF ₂	7.80	8.827	8.33
SrF ₂	10.00	6.151	6.465
$Cd_{0.75}Sr_{0.25}F_2$	8.19	8.714	



The intrinsic breakdown field of the materials is presented in Table 4 and calculated from (8). The E_{BD} are 2.65V/nm, 3.31V/nm and 2.78V/nm for CdF₂, SrF₂ and Cd_{0.75}Sr_{0.25}F₂, respectively, as presented in Table 4. The calculated E_{BD} for SiO_2 is 3.03V/nm, comparable to the experimental value. The E_{BD} for the considered materials is closely the same as SiO₂ (\approx 3V/nm). Most of the proposed oxides for the dielectric layer have $E_{BD} < 2V/nm$ because of their relatively smaller band gaps. There is an improvement in the values of E_{BD} for the fluorides. Fig. 2 shows the relationship between the intrinsic breakdown field (E_{BD}) and band gap (E_g) of fluorides and oxides. The fluorides are CdF₂, SrF₂ and Cd_{0.75}Sr_{0.25}F₂. The oxides are SiO₂ (commonly used dielectric layer) and HfO₂ which is the most attractive oxide among the proposed oxides because of its high value of k (16) [31]. The band gap of HfO₂ is 3.95eV [32]. The graph is linear with E_{BD} directly proportional to Eg. The intrinsic breakdown field increases in the order HfO_2 — CdF_2 — $Cd_{0.75}Sr_{0.25}F_2$ — SiO_2 — SrF_2 . SrF_2 has the highest intrinsic breakdown field because of its highest band gap (9.73eV).

 $\begin{array}{l} \mbox{Table 4. Intrinsic breakdown field E_{BD}} (V/nm) \mbox{ and energy storage} \\ \mbox{ densities F_{ED}} (J/cm^3) \mbox{ of CdF_2}, SrF_2 and $Cd_{0.75}$Sr_{0.25}F_2 \\ \end{array}$

Materials	E _{BD} (V/nm)	$F_{ED}(J/cm^3)$
CdF ₂	2.65	274.83
SrF_2	3.31	298.02
$Cd_{0.75}Sr_{0.25}F_2$	2.78	299.13



Fig. 2 Intrinsic Breakdown Field versus Band gap of Fluorides and Oxides

Fig. 3 presents the graph of energy density F_{ED} of the materials against kE_g^2 . F_{ED} is the electrical energy stored by the insulating layer per unit cm³. Energy density increases in the order HfO₂—SiO₂—CdF₂—SrF₂— Cd_{0.75}Sr_{0.25}F₂. The material with the highest value of F_{ED} is Cd_{0.75}Sr_{0.25}F₂. This is because Cd_{0.75}Sr_{0.25}F₂ has the highest value of kE_g^2 — 584.50(eV)². F_{ED} increases as kE_g^2 increases. Inspite of its high k, F_{ED} is low for HfO₂ because of its low band gap (Eg). The combination of k and E_g are important in determining the quality and reliability of an insulating layer, and the combination will help in the discovery of more usable materials. The electrical energy storage densities are 274.83J/cm³, 298.02J/cm³ and 299.13J/cm³ for CdF₂, SrF₂ and

 $Cd_{0.75}Sr_{0.25}F_2$ respectively. They are calculated from (12) and presented in Table 4. The F_{ED} for the three materials is relatively high, about twice the value for SiO₂ (158.09J/cm³). Although the proposed oxides have relatively high dielectric constants, their energy storage densities and intrinsic breakdown fields are low because of their lower band gaps when compared with those of the fluorides. Based on the investigated intrinsic breakdown field and energy storage density, $Cd_{0.75}Sr_{0.25}F_2$, CdF_2 and SrF_2 are high k dielectrics with improved electrical characteristics.



Fig. 3 Dependence of Energy storage density on kE_g^2 of Fluorides and Oxides

Lattice mismatch of the insulator on the semiconductor is given as $\Delta a/a$. $Cd_{0.75}Sr_{0.25}F_2$ and CdF_2 can be grown on a Gallium Phosphide (GaP) semiconductor. The experimental lattice parameters of $Cd_{0.75}Sr_{0.25}F_2$ and CdF_2 are 5.4778Å and 5.448Å, respectively. For GaP, a=5.45Å [33]. There is a lattice mismatch of 0.88% and 0.50%, respectively, for $Cd_{0.75}Sr_{0.25}F_2$ and CdF_2 , respectively. Since the lattice mismatch is less than 1%, $Cd_{0.75}Sr_{0.25}F_2$ and CdF_2 can be used as insulating layers in GaP-based MIS devices with stable structures. Although CdF_2 has been grown on Si but, there is a problem of a chemical reaction between CdF_2 and GaP in the literatures as far as we know. For SrF_2 , the lattice mismatch is 7%, making the GaP

References

- Q. Zeng et al., "Evolutionary Search for New High k Dielectric Materials: Methodology and Applications to Hafnia Based Oxides," *Acta Crystallography C Structural Chemistry*, vol. 70, pp. 76-84, 2014. [CrossRef] [Google Scholar] [Publisher Link]
- [2] N.S. Sokolov, and S.M. Suturin, "MBE Growth of Calcium and Cadmium Fluoride Nanostructureson Silicon," *Applied Surface Science*, vol. 175, pp. 619-628, 2001. [CrossRef] [Google Scholar] [Publisher Link]
- [3] N.L. Filimonoua, V.A. Iiyushin, and A.A. Velichka, "Molecular Beam Epitaxy of BaF2/CaF2 Buffer Layers on Si(100) Substrate for Monolithic Photoreceivers," *Optoelectronics Instrumentation and Data Processing*, vol. 53, no. 3, pp. 303-308, 2017. [CrossRef] [Google Scholar] [Publisher Link]
- [4] W. Weiss et al., "Surface Morphology of Epitaxial CaF2 and SrF2 Layers Grown on InP(011) Studied by Atomic Force Microscopy and Low Energy Electron Diffraction," *Surface Science*, vol. 268, no. 1-3, pp. 319-324, 1992. [CrossRef] [Google Scholar] [Publisher Link]
- [5] Kazuo Tsutsui et al., "Epitaxial Relations in Ca_xSr_{1-x}F₂ Films Grown on GaAs(111) and Ge(111) Substrates," *Applied Physics Letter*, vol. 46, pp. 1131-1133, 1985. [CrossRef] [Google Scholar] [Publisher Link]

substrate not ideal for the SrF_2 layer. However, the growth of SrF_2 on InP substrate has already been reported [34].

4. Conclusion

In this paper, we used GGA inside the PP-PBE method to investigate the structural and dielectric properties of the cubic alkaline earth fluorides CdF₂, SrF₂, and Cd_{0.75}Sr_{0.25}F₂. The lattice parameter and bulk modulus are determined. To facilitate comparison, the structural characteristics of the alloy's constituent binary compounds were computed. Our calculations and experiments show good agreement. The electronic contribution to the dielectric constant and ionic contribution parameters are calculated using density functional perturbation theory. We computed the intrinsic breakdown field and energy storage density for CdF₂, SrF₂, and Cd_{0.75}Sr_{0.25}F₂. The calculations allowed us to identify Cd_{0.75}Sr_{0.25}F₂ as a better material for insulating layers in GaPbased MIS systems. CdF₂ is likewise applicable, although SrF₂ cannot be grown on GaP substrate due to a large lattice mismatch. It is worth noting that κ is important in the choice of dielectric material.

However, band gap energy is also crucial because barrier height increases with increasing band gap, and as k increases, band gap decreases. To minimize leakage current, a large barrier height is essential. Thus, a balance must be ensured between k, and E_g . Energy storage density of $Cd_{0.75}Sr_{0.25}F_2$ is closely two times greater than SiO₂. Their E_{BD} are closely equal. The intrinsic breakdown field increases in the order HfO_2 — CdF_2 — $Cd_{0.75}Sr_{0.25}F_2$ — SiO_2 — SrF_2 while the Energy density increases in the order HfO2-SiO2-CdF2-SrF2- $Cd_{0.75}Sr_{0.25}F_2$. Since a high κ material does not necessarily result in high energy density and high intrinsic breakdown field, more materials can be discovered for application as dielectrics in MIS devices by carefully looking at their dielectric constants as well as their band gaps. This study stimulates the design and construction of GaP-based MIS devices with a Cd_{0.75}Sr_{0.25}F₂ insulating layer.

Acknowledgement

The authors thanked Caleb University Lagos, for the provision of internet facilities and research motivation

- [6] Motoki Maeda et al., "Crystalline structure of Epitaxial Ca_xMg_{1-x}F2 alloys on Si(100) and (111) substrates," *Thin Solid Films*, vol. 515, no. 2, pp. 448-451, 2006. [CrossRef] [Google Scholar] [Publisher Link]
- [7] I.I. Buchinskaya, and P.P. Fedorov, "A new Optical Medium-Cd_{0.75}Sr_{0.25}F2 single crystals," *Crystallography Reports*, vol. 49, no. 2, pp. 279-281, 2004. [CrossRef] [Google Scholar] [Publisher Link]
- [8] Donald C. Stockbarger, "The Production of Large Single Crystals Of Lithium Fluorides," *Review of Science Instrumentation*, vol. 7, pp. 133-1135, 1936. [CrossRef] [Google Scholar] [Publisher Link]
- [9] V.V. Novikov et al., "Anharmonicity of Lattice Vibrations and the Thermal Properties of Cd_{1-x}Sr_xF₂ Solid Solutions," *Physics of Solid State*, vol. 62, no. 4, pp. 714-721, 2020. [CrossRef] [Google Scholar] [Publisher Link]
- [10] V.V. Novikov et al., "Structural Disorder and Heat Capacity of a Solid Solution between Cadmium and Strontium Fluorides," *Inorganic Materials*, vol. 56, no. 6, pp. 626-632, 2020. [CrossRef] [Google Scholar] [Publisher Link]
- [11] N.I. Sorokin et al., "Electrical and Thermal Conductivities of Congruently Melting Single Crystals of Isovalent M_{1-x}M'_xF₂ solid solutions (M, M'=Ca,Sr,Cd,Pb) in Relation to their Defect Fluorite Structure," *Crystallography Reports*, vol. 60, no. 4, pp. 532-536, 2015.
 [CrossRef] [Google Scholar] [Publisher Link]
- [12] D.N. Karimov et al., "Crystal Growth and Thermal Conductivity of the Congruently Melting Solid Solution Cd_{0.77}Sr_{0.23}F2," *Inorganic Materials*, vol. 55, no. 5, pp. 495-499, 2019. [CrossRef] [Google Scholar] [Publisher Link]
- [13] P.A. Popov et al., "Thermophysical Characteristics of Ca_{1-x}Sr_xF2 Solid Solution Crystal (0≤x≤1)," Crystallography Reports, vol. 60, no. 1, pp. 116-122, 2015. [CrossRef] [Google Scholar] [Publisher Link]
- [14] Atsushi Kawamoto, Kyeongjae Cho, and Robert Dutton, "Perspectives Paper: First Principles Modeling Of High-K Gate Dielectrics," Journal of Computer Aided Materials Design, vol. 8, pp. 39-57, 2001. [CrossRef] [Google Scholar] [Publisher Link]
- [15] Paolo Giannozzi et al., "Quantum Espresso: A Modular and Open-Source Software Project for Quantum Simulations of Materials," *Journal of Physics: Condensed Matter*, vol. 21, no. 39, pp. 395502-395520, 2009. [Google Scholar] [Publisher Link]
- [16] John P. Perdew, Kieron Burke, and Matthias Ernzerhof, "Generalized Gradient Approximation Made Simple," *Physical Review Letter*, vol. 77, no. 18, pp. 3865-3868, 1996. [CrossRef] [Google Scholar] [Publisher Link]
- [17] Hendrik J. Monkhorst, and James D. Pack, "Special Points for Brillouin-Zone Integrations," *Physical Review B*, vol. 13, no. 12, pp. 5188-5192, 1976. [CrossRef] [Google Scholar] [Publisher Link]
- [18] F.D. Murnaghan, "The Compressibility of Media under Extreme Pressures," Proceedings of the National Academy of Sciences of the United States of America, vol. 30, no. 9, pp. 244-247, 1944. [CrossRef] [Google Scholar] [Publisher Link]
- [19] Vesselin Dimitrov, and Sumio Sakka, "Electronic Oxide Polarizability and Optical Basicity of Simple Oxides," *Journal of Applied Physics*, vol. 79, pp. 1736-1740, 1996. [CrossRef] [Google Scholar] [Publisher Link]
- [20] P. Hervé, and L.K.J. Vandamme, "General Relation between Refractive Index and Energy gap in Semiconductors," *Infrared Physics and Technology*, vol. 35, no. 4, pp. 609-615, 1994. [CrossRef] [Google Scholar] [Publisher Link]
- [21] Li-Mo Wang, "Relationship between Intrinsic Breakdown field and Band gap of Materials," 2006 25th International Conference on Microelectronics, Belgrade, Serbia, pp. 576-579, 2006. [CrossRef] [Google Scholar] [Publisher Link]
- [22] Hiroshi Kamimura, Pallab Bhattacharya, and Roberto Fornari, Comprehensive Semiconductor Science and Technology, 1st ed., Elsevier Science, Amsterdam, 2011. [Google Scholar] [Publisher Link]
- [23] G.A. Samara, "Temperature and Pressure Dependence of the Dielectric Properties of PbF2 and the Alkaline-Earth Fluorides," *Physical Review B*, vol. 13, no. 10, pp. 4529-4544, 1976. [CrossRef] [Google Scholar] [Publisher Link]
- [24] S. Alterovitz, and D. Gerlich, "Third-Order Elastic Moduli of Strontium Fluoride," *Physical Review B*, vol. 1, no. 6, pp. 2718-2223, 1970. [CrossRef] [Google Scholar] [Publisher Link]
- [25] L. Rodriguez de Marcus et al., "Optical Constants of SrF₂ thin films in the 25-780eV spectral range," *Journal of Applied Physics*, vol. 113, no. 14, pp. 143501-143527, 2013. [CrossRef] [Google Scholar] [Publisher Link]
- [26] A.A. Pronkin, L.N. Urosovskaya, and N.A. Makarenko, "Use of Cadmium Fluoride to Produce High Refractive Index Glasses," *The Soviet Journal of Glass Physics and Chemistry*, vol. 9, no. 2, pp. 158-161, 1983. [Publisher Link]
- [27] B.A. Orlowski, and P. Plenkiewicz, "Electronic Band Structure of CdF2: Photoemission Experiment and Pseudopotential Calculations," *Physical Status Solid B*, vol. 126, no. 1, pp. 285-292, 1984. [CrossRef] [Google Scholar] [Publisher Link]
- [28] K. Suzuki et al., "Band Gap Engineering of Ca_xSr_{1-x}F2 and its Application as Filterless Vacuum Ultraviolet Photodetectors with Controllable Spectra Responses," *Optical Materials*, vol. 88, pp. 576-579, 2019. [CrossRef] [Google Scholar] [Publisher Link]
- [29] K.F. Young, and H.P.R. Frederikse, "Temperature and Pressure Dependent of Dielectric Constant of Cadmium Fluoride," *Journal of Applied Physics*, vol. 40, pp. 3115-3118, 1969. [CrossRef] [Google Scholar] [Publisher Link]
- [30] Carl Andeen, John Fontanella, and Donald Schuele, "Low-Frequency Dielectric Constants of the Alkaline Earth Fluorides by the Method of Substitution," *Journal of Applied Physics*, vol. 42, no. 6, pp. 2216-2219, 1971. [CrossRef] [Google Scholar] [Publisher Link]
- [31] Xinyuan Zhao, and David Vanderbilt, "First-Principles Study of Structural, Vibrational and Lattice Dielectric Properties of Hafnium Oxide," *Physical Review B*, vol. 65, no. 23, pp. 233106-233109, 2002. [CrossRef] [Google Scholar] [Publisher Link]

- [32] Hong Jiang et al., "Electronic Band Structure of Zirconia and Hafnia Polymorphs from the GW Perspective," *Physical Review B*, vol. 81, no. 8, pp. 85119-85127, 2010. [CrossRef] [Google Scholar] [Publisher Link]
- [33] Robert C. Weast, CRC Handbook of Chemistry and Physics, 62nd ed., CRC Press, New York, 1981. [Google Scholar] [Publisher Link]
- [34] S. Heun et al., "Morphology of thin SrF2 films on InP (111) Studied by Reflection High-Energy Electron Diffraction," *Journal of Crystal Growth*, vol. 150, no. 2, pp. 108-114, 1995. [CrossRef] [Google Scholar] [Publisher Link]